$$f(x, y) \left[ \frac{d^m y}{dx^m} \right]^p + \phi(x, y) \left[ \frac{d^{m-1}(y)}{dx^{m-1}} \right]^q + \dots = 0 \text{ is order } m \& \text{ degree } p.$$

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(i) 
$$x dx + y dy = r dr$$
 (ii)  $dx^2 + dy^2 = dr^2 + r^2 d\theta^2$  (iii)  $x dy - y dx = r^2 d\theta$ 

**TYPE-2:** 
$$\frac{dy}{dx} = f(ax + by + c), b \neq 0.$$

Get Solution of These Packages & Learn by Video Tutorials on www.Matt Consider the example  $(x + y)^2 \frac{dy}{dx} = a^2$ . TYPE-3. HOMOGENEOUS EQUATIONS: A differential equation of the form  $\frac{dy}{dx} = \frac{f(x,y)}{\phi(x,y)}$ where  $f(x,y) \& \phi(x,y)$  are homogeneous functions of x & y, and of the sa Homogeneous . This equation may also be reduced to the form  $\frac{dy}{dx} = g$ putting y = vx so that the dependent variable y is changed to another variable unknown function, the differential equation is transformed to an equation with Consider  $\frac{dy}{dx} + \frac{y(x+y)}{x^2} = 0$ . TYPE-4. EQUATIONS REDUCIBLE TO THE HOMOGENEOUS FORM: If  $\frac{dy}{dx} = \frac{a_1x + b_1y + c_1}{x^2}$ ; where  $a_1b_2 - a_2b_1 \neq 0$ , i.e.  $\frac{a_1}{b_1} \neq \frac{a_2}{b_1}$ the nesubstitution  $x = u + b_1 y = v + k$  transform this equation to a homogeneous variables u and v where h and k are arbitrary constants to be chosen so as equation homogeneous which can be solved by the method as given in Ty aution homogeneous which can be solved by the method as given in Ty with variables superable. and (ii)  $b_1 + a_2 = 0$ , then a substitution  $u = a_1 + b_1 y$  transforms the differential equa with variables superable. The result easily. Consider  $\frac{dx}{dx} = \frac{x - 2y + y - 1}{2x + 2y + 1}$ ;  $\frac{dy}{dx} = \frac{2x + 3y + 1}{4x + 6y - 5}$  &  $\frac{dy}{dx} = \frac{2x - y + 1}{6x - 5y + 4}$ . (iii) Lancequation of the form: y(xy) dx + xg(xy) dy = 0 the variables can be separate xy = v. THONTAINT NOTE : (iii) The function of the gram: y(x') dx + xg(xy) dy = 0 the variables x is differential equation homogeneous which y'' = y''(x, y) = f(x, y). The function of degree n,  $f(x, y) = ax^{24} + bx^{2} + b^{2} + b^{2}$  is a homogeneous function of degree n,  $f(x, y) = ax^{24} + bx^{2} + b^{2} + b^$ of 35 where  $f(x, y) & \phi(x, y)$  are homogeneous functions of x & y, and of the same degree, is called  $\mathbf{\Sigma}$ **HOMOGENEOUS**. This equation may also be reduced to the form  $\frac{dy}{dx} = g\left(\frac{x}{y}\right)$  & is solved by putting y = vx so that the dependent variable y is changed to another variable v, where v is some unknown function, the differential equation is transformed to an equation with variables separable. 0 98930 58881.

then the substitution x = u + h, y = v + k transform this equation to a homogeneous type in the new  $\sigma$ variables u and v where h and k are arbitrary constants to be chosen so as to make the given k equation homogeneous which can be solved by the method as given in Type-3. If equation homogeneous which can be solved by the method as given in Type -3. If  $a_1b_2-a_2b_1=0$ , then a substitution  $u = a_1x + b_1y$  transforms the differential equation to an equation  $\bigotimes_{i=1}^{n} with variables separable, and$ 

with variables separable. and  $b_1 + a_2 = 0$ , then a simple cross multiplication and substituting d(xy) for x dy + y dx & integrating 0 term by term yields the result easily. Consider  $\frac{dy}{dx} = \frac{x - 2y + 5}{2x + y - 1}$ ;  $\frac{dy}{dx} = \frac{2x + 3y - 1}{4x + 6y - 5}$  &  $\frac{dy}{dx} = \frac{2x - y + 1}{6x - 5y + 4}$ In an equation of the form: yf(xy) dx + xg(xy)dy = 0 the variables can be separated by the substitution  $\frac{dy}{dx} = \frac{2x - y + 1}{6x - 5y + 4}$ 

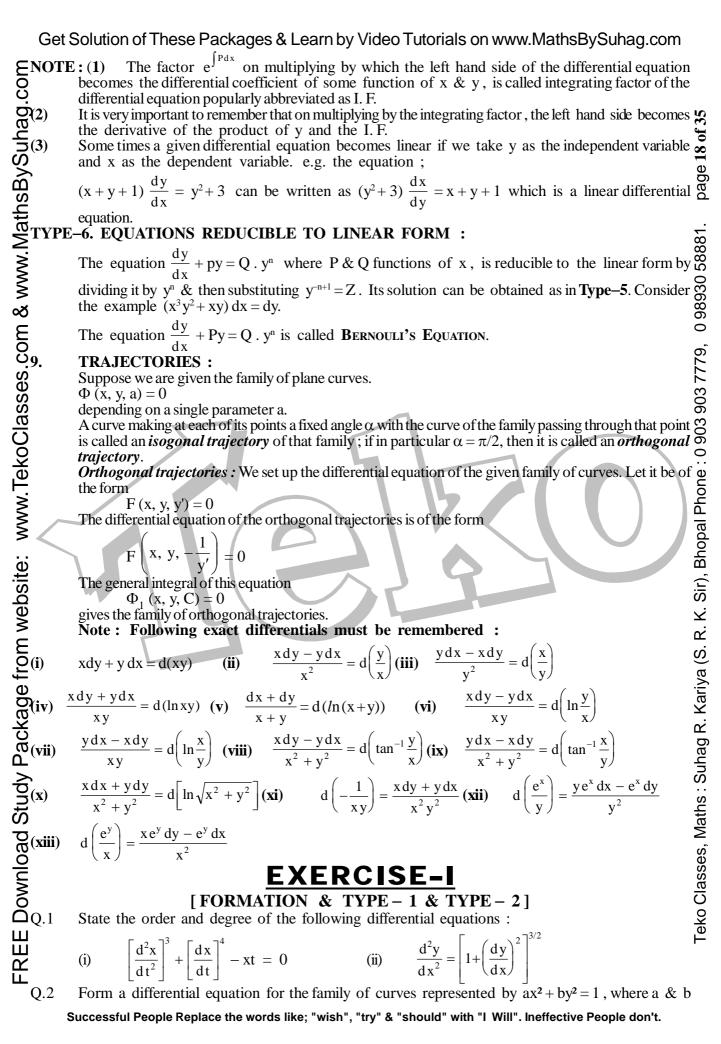
Consider 
$$\frac{dy}{dx} = \frac{x - 2y + 5}{2x + y - 1}$$
;  $\frac{dy}{dx} = \frac{2x + 3y - 1}{4x + 6y - 5}$  &  $\frac{dy}{dx} = \frac{2x - y + 1}{6x - 5y + 4}$ 

Sir), Bhopal The function f(x, y) is said to be a homogeneous function of degree n if for any real number  $t (\neq 0)$ , we have  $f(tx, ty) = t^n f(x, y)$ . For e.g.  $f(x, y) = ax^{2/3} + hx^{1/3}$ .  $y^{1/3} + by^{2/3}$  is a homogeneous function of degree 2/3.

A differential equation of the form  $\frac{dy}{dx} = f(x, y)$  is homogeneous if f(x, y) is a homogeneou s Ä

$$a_0(x) \frac{d^n y}{dx^n} + a_1(x) \frac{d^{n-1} y}{dx^{n-1}} + \dots + a_n(x) \cdot y = \phi(x)$$
. Where  $a_0(x)$ ,  $a_1(x) \dots a_n(x)$  are called the  $\frac{d^n y}{dx^n}$ 

 $\int_{a} (x) + Py = 0$ is not depend on the first of the f



### Get Solution of These Packages & Learn by Video Tutorials on www.MathsBySuhag.com are arbitary constants.

Obtain the differential equation of the family of circles  $x^2 + y^2 + 2gx + 2fy + c = 0$ ; where 

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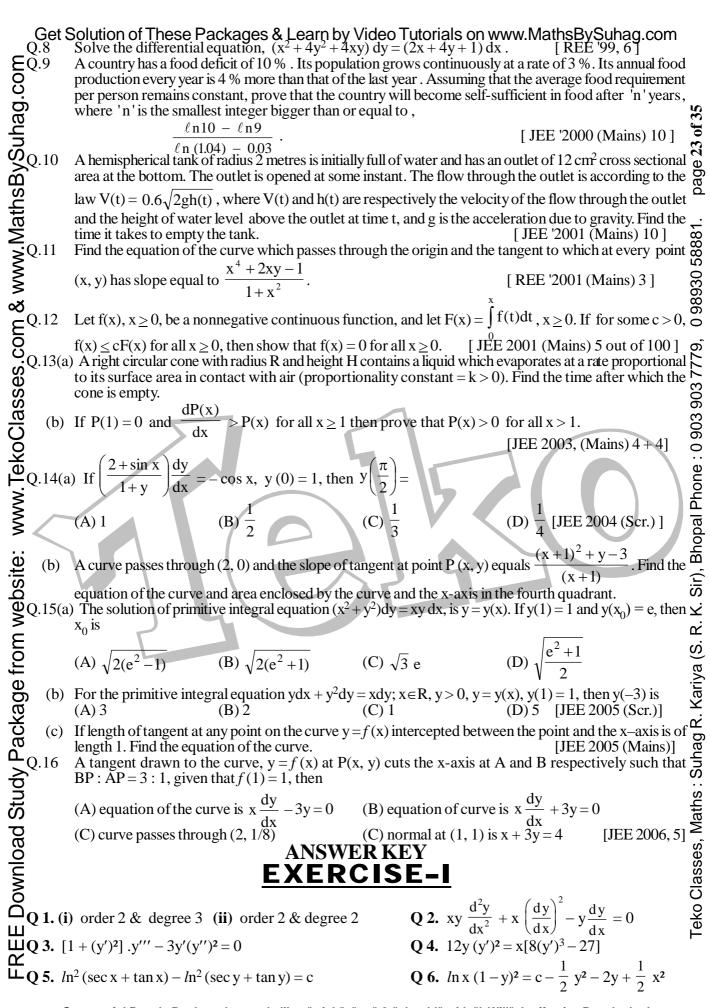
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 < g, f & c are arbitary constants. Form the differential equation of the family of curves represented by,  $c (y+c)^2 = x^3$ ; where c is any arbitrary constant. page 19 of 35  $\frac{\ln (\sec x + \tan x)}{\cos x} dx = \frac{\ln (\sec y + \tan y)}{\cos y} dy \qquad Q.6 \qquad (1 - x^2) (1 - y) dx = xy (1 + y) dy$  $\frac{dy}{dx} + \frac{\sqrt{(x^2 - 1)(y^2 - 1)}}{xy} = 0$ Q.8  $y - x \frac{dy}{dx} = a\left(y^2 + \frac{dy}{dx}\right)$   $\frac{x \, dx - y \, dy}{x \, dy - y \, dx} = \sqrt{\frac{1 + x^2 - y^2}{x^2 - y^2}}$ Q.10  $\frac{dy}{dx} = \sin(x + y) + \cos(x + y)Q.11$   $\frac{dy}{dx} = \frac{x(2\ln x + 1)}{\sin y + y \cos y}$  $\frac{dy}{dx} = \frac{x(2\ln x + 1)}{\sin y + y\cos y}$ It is known that the decay rate of radium is directly proportional to its quantity at each given instant. Find the law of variation of a mass of radium as a function of time if at t = 0, the mass of the radius to and during time t<sub>0</sub>  $\alpha$  % of the original mass of radium 1 It is known that the decay rate of radium is directly proportional to its quantity at each given instant. Find the law of variation of a mass of radium as a function of time if at t = 0, the mass of the radius was  $m_0$  and during time  $t_0 \alpha$ % of the original mass of radium decay.  $\frac{dy}{dx} + \sin \frac{x+y}{2} = \sin \frac{x-y}{2}$ Q.14 Sin x.  $\frac{dy}{dx} = y$ . *l*ny if y = e, when  $x = \frac{\pi}{2}$  $\frac{\mathrm{d}y}{\mathrm{d}x} + \sin\frac{x+y}{2} = \sin\frac{x-y}{2}$ Q.14 Sin x.  $\frac{dy}{dx} = y \cdot lny$  if y = e, when  $x = \frac{\pi}{2}$  $e^{(dy/dx)} = x + 1$  given that when x = 0, y = 3A normal is drawn at a point P(x, y) of a curve. It meets the x-axis at Q. If PQ is of constant length k, then show that the differential equation describing such curves is,  $y\frac{dy}{dx} = \pm \sqrt{k^2 - y^2}$ . Find the  $\bigotimes$ equation of such a curve passing through (0, k). Find the curve for which the sum of the lengths of the tangent and subtangent at any of its point  $\overset{\circ}{\mathbf{0}}$  is proportional to the product of the co-ordinates of the point of tangent at any of its point  $\overset{\circ}{\mathbf{0}}$ is proportional to the product of the co-ordinates of the point of tangency, the proportionality factor is  $\circ$ . equal to k. K. Sir), Bhopal Phone Obtain the differential equation associated with the primitive,  $y = c_1 e^{3x} + c_2 e^{2x} + c_3 e^x$ , where  $c_1$ ,  $c_2$ ,  $c_3$  are arbitrary constants. A curve is such that the length of the polar radius of any point on the curve is equal to the length of the tangent drawn at this point. Form the differential equation and solve it to find the equation of the curve. Find the curve y = f(x) where  $f(x) \ge 0$ , f(0) = 0, bounding a curvilinear trapezoid with the base [0, x] whose area is proportional to (n + 1)<sup>th</sup> power of f(x). It is known that f(1) = 1. **EXERCISE-II** [ TYPE-3 & TYPE-4] Ľ.  $\frac{\mathrm{d}\,\mathrm{y}}{\mathrm{d}\,\mathrm{x}} = \frac{\mathrm{x}^2 + \mathrm{x}\mathrm{y}}{\mathrm{x}^2 + \mathrm{y}^2}$ Ś Find the equation of a curve such that the projection of its ordinate upon the normal is equal to its abscissa. The light rays emanating from a point source situated at origin when reflected from the mirror of a search light are reflected as beam parallel to the x-axis. Show that the surface is parabolic, by first forming the  $\overline{x}$ differential equation and then solving it. The perpendicular from the origin to the tangent at any point on a curve is equal to the abscissa of the point  $\dot{\mathbf{r}}$ of contact. Find the equation of the curve satisfying the above condition and which passes through (1, 1). Find the equation of the curve intersecting with the x- axis at the point x = 1 and for which the length of  $\frac{2}{3}$ the subnormal at any point of the curve is equal to the arthemetic mean of the co-ordinates of this point  $\vec{o}$  $\frac{y}{dx} - a - x \text{ to reduce the equation } y^3 \cdot \frac{dy}{dx} + x + y^2 = 0 \text{ to homogeneous form and} \\ \frac{y}{dx} + x + y^2 + y^$  $(y-x)^2(x+2y) = 1$ .  $\left| x\cos\frac{y}{x} + y\sin\frac{y}{x} \right| y - \left| y\sin\frac{y}{x} - x\cos\frac{y}{x} \right| x\frac{dy}{dx} = 0$ 

Get Solution of These Packages & Learn by Video Tutorials on www.MathsBySuhag.com 2.11 Find the curve for which any tangent intersects the y-axis at the point equidistant from the point of 0.11 of 35 x + y = 0 & 2x + y + 1 = 0. If the normal drawn to a curve at any point P intersects the x-axis at G and the perpendicular from P on  $\begin{bmatrix} 0 \\ 0 \\ 0 \end{bmatrix}$  the x-axis meets at N. such that the sum of the lengths of PC and NC the x-axis meets at N, such that the sum of the lengths of PG and NG is proportional to the abscissa of the point P, the constant of proportionality being k. Form the differential equation and solve it to show that the equation of the curve is,  $y^2 = cx^{\frac{1}{k}} - \frac{k^2 x^2}{2k-1}$  or  $y^2 = \frac{k^2 x^2}{2k+1} - cx^{-\frac{1}{k}}$ , where c is any arbitrary  $\frac{80}{20}$ Sir), Bhopal Phone : 0 903 903 7779, 0 98930 Ŀ. Ř Feko Classes, Maths : Suhag R. Kariya (S.

Get Solution of These Packages & Learn by Video Tutorials on www.MathsBySuhag.com Q.24 Find the curve for which the area of the triangle formed by the x-axis, the tangent line and radius vector of the point of tangency is equal to a<sup>2</sup>. Q.25 Attack contains 100 thres of fresh water. A solution containing 1 grivfitre of soluble lawn fertilizer truss into the tank at the rate of 1 librini, and the mixture is pumped out of the tank at the rate of 3 libres/min. Find the time when the amount of fertilizer in the tank is in aximum. Find the time when the amount of fertilizer in the tank is in aximum. (GENERAL - CHANCE OF VARIABLE BY A SUTTABLE SUBSTITUTION) Q.1.  $(x - y^3) dx + 2xy dy = 0$  Q.2.  $(x^1 + y^1 + 2) dx + 2y dy = 0$ Q.3.  $x \frac{dy}{dx} + y \ln y = xye<sup>3</sup> Q.4 \frac{dy}{dx} - \frac{11 + x}{1 + x} = (1 + x) e<sup>3</sup> sec yQ.5. <math>\frac{dy}{dx} = \frac{e^2}{x^2} - \frac{1}{x}$ Q.6.  $\left(\frac{dy}{dx}\right)^2 - (x + y) \frac{dy}{dx} + xy = 0 Q.7. \frac{dy}{dx} = \frac{y^2 - x}{y(x + 1)} Q.8. (1 - xy + x^2y^2) dx = x^2 dy$  $\frac{dy}{dx} = e^{x-2} (e^{x} - e^{x}) Q.10. yy' sin x = \cos x (sin x - y^2)$ **EXERCISE-V**(MISCELLANEOUS) GQ.1  $\frac{dy}{dx} - y \ln 2 = 2^{sin x}$ . (cos x - 1) h2, y being bounded when  $x \to + \infty$ . (0, 12). The tangents drawn to both curves at the points (0, 1) &  $y = \int_{1}^{2} f(t) dt$  passing through the points. (0, 12). The tangents drawn to both curves at the points with equal abscissas intersect on the x-axis. Find the curve f(x). (1) the dy arc containts such that the linear combinations  $\alpha + u(x) + \beta + v(x)$  is a solution of the given equation find the relation detween (x - a)(1) f(x) is the third particular solution of given equation (x) and v(x) are known, find the reneral solution of the given equation in terms of (u') and (v'). (1) f(x) is be which passes through the point (2, 0) such that the segment of the tangent between the point of tangency & the y-axis has a constant length equal to 2. (2)  $x^3 \frac{dy}{dx} = y^4 \frac{x^4}{x^4} + \frac{y^4}{y^2} = 0. Q.8$   $\frac{ydx - x^4}{(x - y)^2} = \frac{dx}{2\sqrt{1 - x^2}}$ , given that y = 2 when x = 1Get Solution of These Packages & Learn by Video Tutorials on www.MathsBySuhag.com 2.24 Find the curve for which the area of the triangle formed by the x-axis, the tangent line and radius vector page 21 of 35 K. Sir), Bhopal Phone : 0 903 903 7779, 0 98930 58881. Teko Classes, Maths : Suhag R. Kariya (S. R.  $\bigcup_{x \neq 1} Q.14$  Find the integral curve of the differential equation,  $x(1-x \ln y)$ .  $\frac{dy}{dx} + y = 0$  which passes through  $\left(1, \frac{1}{e}\right)$ Find all the curves possessing the following property; the segment of the tangent between the point of tangency & the x-axis is bisected at the point of intersection with the y-axis.

 $Q.16 \quad y^2(y\,dx + 2x\,dy) - x^2(2y\,dx + x\,dy) = 0$ Successful People Replace the words like; "wish", "try" & "should" with "I Will". Ineffective People don't.



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$$Q 0, \sqrt{x^2 - 1} - \sec^{-1} x + \sqrt{y^2 - 1} = c$$
 $Q 8, y = c (1 - ay) (x + a)$ 
 $Q 9, \sqrt{x^2 - y^2} + \sqrt{1 + x^2 - y^2} = \frac{c(x + y)}{c(x^2 - y^2)}$ 
 $Q 10, \ln \left[1 + \tan \frac{x + y}{2}\right] = x + c$ 
 $Q 12, m = m_0 e^{-kt}$  where  $k = -\frac{1}{t_0} \ln \left(1 - \frac{\alpha}{100}\right)$ 
 $Q 13, \ln \left| \tan \frac{y}{4} \right| = c - 2 \sin \frac{x}{2}$ 
 $Q 14, y = e^{\tan(x2)}$ 
 $Q 15, y = (x + 1), \ln (x + 1)^{-} x + 3$ 
 $Q 16, x^2 + y^2 = k^2$ 
 $Q 17, y = \frac{1}{k} \ln \left[ (k^2 x^2 - 1) \right]$ 
 $Q 18, \frac{d^3y}{dx^2} - 6\frac{d^3y}{dx^2} + 11\frac{dy}{dx} - 6y = 0$ 
 $Q 20, \frac{y^2 \pm y\sqrt{y^2 - x^2}}{x^2} = \ln \left[ \left( y \pm \sqrt{y^2 - x^2} \right) \cdot \frac{c^2}{x^3} \right]$ 
where exp  $x = e^x$ 
 $\frac{1}{k} \ln \left[ x^2 + y^2 - 1 - 10^{-1} \left( \frac{\pi}{3} \right) = c$ , where  $a = x + y^2$ 
 $Q 1, x = c y^2 + 2y - 2x = c$ 
 $Q 2, \frac{y^2 \pm y\sqrt{y^2 - x^2}}{x^2} = \ln \left[ \left( y \pm \sqrt{y^2 - x^2} \right) \cdot \frac{c^2}{x^3} \right]$ 
where same sign has to be taken.
 $\frac{2y + 1}{x^2 + y^2 - 2x = 0}$ 
 $Q 5, (x - y)^2 (x + 2y) = 1$ 
 $Q 10, xy \cos \frac{y}{x} = c$ 
 $Q 10, xy \cos \frac{y}{x} = c$ 
 $Q 11, x^2 + y^2 = cx$ 
 $Q 10, xy \cos \frac{y}{x} = c$ 
 $Q 12, \arctan \frac{2y + 1}{x^2 + 4} = \ln c \sqrt{x^2 + y^2 + x + y + \frac{1}{2}}$ 
 $Q 13, (x + y^2) = c (y - x)^3$ 
 $Q 14, \tan^{-1} \frac{y + 3}{x + 2} + \ln c \sqrt{(y + 3)^2 + (x + 2)^2} = 0$ 
 $Q 10, xy \cos \frac{y}{x} = c$ 
 $Q 11, x^2 + y^2 = cx$ 
 $Q 12, \arctan \frac{2y + 1}{x + 4} = \ln c \sqrt{x^2 + y^2 + x + y + \frac{1}{2}}$ 
 $Q 14, \tan^{-1} \frac{y + 3}{x + 2} + \ln c \sqrt{(y + 3)^2 + (x + 2)^2} = 0$ 
 $Q 10, xy \cos \frac{y}{x} = c$ 
 $Q 11, x^2 + y^2 = cx$ 
 $Q 14, \tan^{-1} \frac{y + 3}{x + 2} + \ln c \sqrt{(y + 3)^2 + (x + 2)^2} = 0$ 
 $Q 14, \tan^{-1} \frac{y + 3}{x + 2} + \ln c \sqrt{(y + 3)^2 + (x + 2)^2} = 0$ 
 $Q 14, \tan^{-1} \frac{y + 3}{x + 2} + \frac{1}{2} \ln \sqrt{1 + \frac{x^2}{x}} = 0$ 
 $Q 14, \tan^{-1} \frac{y + 3}{x + 2} + \frac{1}{2} \ln \sqrt{1 + \frac{x^2}{x}} = 0$ 
 $Q 14, \tan^{-1} \frac{y + 3}{x + 2} + \frac{1}{2} \ln \sqrt{1 + \frac{x^2}{x}} = 0$ 
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 $Q 14, \tan^{-1} \frac{y + 3}{x + 2} + \frac{1}{2} \ln \sqrt{1 + \frac{x^2}{x}} = 0$ 
 $Q 14, \tan^{-1} \frac{y +$ 

# **EXERCISE-VII**

**EXERCISE-VII**  
**EXERCISE-VII**  
**I** The degree of differential equation satisfying the relation  

$$\sqrt{1+x^2} + \sqrt{1+y^2} = \lambda (x \sqrt{1+y^2} - y \sqrt{1+x^2})$$
 is :  
(A) 1 (B) 2 (C) 3 (D) none of these  
(A) 1 (B)  $p = q$  (C)  $p \ge q$  (D) none of these  
(A)  $p < q$  (B)  $p = q$  (C)  $p \ge q$  (D) none of these  
(A)  $(y - x\frac{dy}{dx})^2 = 1 - (\frac{dy}{dx})^2$  (B)  $(y + x\frac{dy}{dx})^2 = 1 - (\frac{dy}{dx})^2$   
(C)  $(y - x\frac{dy}{dx})^2 = 1 - (\frac{dy}{dx})^2$  (B)  $(y + x\frac{dy}{dx})^2 = 1 - (\frac{dy}{dx})^2$   
(C)  $(y - x\frac{dy}{dx})^2 = 1 - (\frac{dy}{dx})^2$  (D)  $(y - x\frac{dy}{dx})^2 = 1 - (\frac{dy}{dx})^2$   
(C)  $(y - x\frac{dy}{dx})^2 = 1 - (\frac{dy}{dx})^2$  (D)  $(y - x\frac{dy}{dx})^2 = 1 - (\frac{dy}{dx})^2$   
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(C)  $(y - x\frac{dy}{dx})^2 = 1 - (\frac{dy}{dx})^2$  (D)  $(y - x\frac{dy}{dx})^2 = 1 - (\frac{dy}{dx})^2$   
(C)  $(y - x\frac{dy}{dx})^2 = 1 - (\frac{dy}{dx})^2$  (D)  $(y - x\frac{dy}{dx})^2 = 1 - (\frac{dy}{dx})^2$   
(D)  $(y - x\frac{dy}{dx})^2 = 1 - (\frac{dy}{dx})^2$   
(C)  $(y - x\frac{dy}{dx})^2 = 1 - (\frac{dy}{dx})^2$  (D)  $(y - x\frac{dy}{dx})^2 = 1 - (\frac{dy}{dx})^2$   
(C)  $(1 + (\frac{dy}{dx})^2)^3 = a^2 \frac{d^2y}{dx^2}$  (B)  $(1 + (\frac{dy}{dx})^2)^3 = a^2 (\frac{d^2y}{dx^2})^2$   
(D) none of these  
(A)  $(x^2 - y)^2 \frac{dy}{dx} - 2xy = 0$  (B)  $(x^2 - y)^3 \frac{dy}{dx} + 2xy = 0$   
(C)  $(x^2 - y)^2 \frac{dy}{dx} - xy = 0$  (D)  $(x^2 - y^2) \frac{dy}{dx} + xy = 0$   
(C)  $(x^2 - y^2) \frac{dy}{dx} - xy = 0$  (D)  $(x^2 - y^2) \frac{dy}{dx} + xy = 0$   
(C)  $(x^2 - x^2) \frac{dy}{dx} - xy = 0$  (D)  $(x^2 - y)^3 \frac{dy}{dx} + xy = 0$   
(C)  $(x^2 - x^2) \frac{dy}{dx} - xy = 0$  (D)  $(x^2 - y)^3 \frac{dy}{dx} + xy = 0$   
(C)  $(x^2 - x^2) \frac{dy}{dx} - xy = 0$  (D)  $(x^2 - y) \frac{dy}{dx} + xy = 0$   
(C)  $(x^2 - x^2) \frac{dy}{dx} - xy = 0$  (D)  $(x^2 - y) \frac{dy}{dx} + xy = 0$   
(C)  $(x^2 - x^2) \frac{dy}{dx} - xy = 0$  (D)  $(x^2 - y) \frac{dy}{dx} + xy = 0$   
(D)  $(x^2 - y) \frac{dy}{dx} + 1 + x + y + xy$  and  $y = 0$  when  $x = 5$ , the value of  $x$  for  $y = 3$  is  $(x - x)^2 - (x - x$ 

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(A) 
$$y = Ae^{in} (2a - x) \sqrt{x + a}$$
 (B)  $y = Ae^{ina} (a - x) \sqrt{x + a}$   
(C)  $y = Ae^{ina} (2a + x) \sqrt{x + a}$  (D)  $y = Ae^{ina} (2a - x) \sqrt{x + a}$   
Where A is an arbitrary constant.  
(A)  $\frac{dy}{dx} + f(x) = 0$  (B)  $\frac{dy}{dx} + y(x) = f(x)$  then  $y_i(x) + y_i(x)$  is solution of :  
(A)  $\frac{dy}{dx} + f(x) = 0$  (B)  $\frac{dy}{dx} + y(x) = f(x)$  then  $y_i(x) + y_i(x)$  is solution of :  
(A)  $\frac{dy}{dx} + f(x) = 0$  (B)  $\frac{dy}{dx} + y(x) = f(x)$  (D)  $\frac{dx}{dx} + f(x) = 2f(x)$   
(C)  $\frac{dy}{dx} + f(x) = 0$  (B)  $\frac{d^2x}{dt^2} + n^2 x = 0$  (C)  $\frac{d^2x}{dt^2} - n^2 x = 0$  (D)  $\frac{d^2x}{dt^2} + \frac{1}{n^2} x = 0$ .  
(A)  $\frac{d^2x}{dt^2} + nx = 0$  (B)  $\frac{d^2x}{dt^2} + n^2 x = 0$  (C)  $\frac{d^2x}{dt^2} - n^2 x = 0$  (D)  $\frac{d^2x}{dt^2} + \frac{1}{n^2} x = 0$ .  
(A)  $\frac{d}{dt} = 2f(0) \cot 0 = 0$  (B)  $\frac{d}{dt} - 2f(0) \cot 0 = 0$  (C)  $\frac{d}{dt} + 2f(0) = 0$  (D)  $\frac{d}{dt} - 2f(0) = 0$   
(A)  $\frac{d}{dt} - 2f(0) \cot 0 = 0$  (B)  $\frac{d}{dt} - 2f(0) \cot 0 = 0$  (C)  $\frac{d}{dt} + 2f(0) = 0$  (D)  $\frac{d}{dt} - 2f(0) = 0$   
(A)  $\frac{d}{dt} - 2f(0) \cot 0 = 0$  (B)  $\frac{d}{dt} - 2f(0) \cot 0 = 0$  (C)  $\frac{d}{dt} + 2f(0) = 0$  (D)  $\frac{d}{dt} - 2f(0) = 0$   
(A)  $\frac{d}{dt} - 2f(0) \cot 0 = 0$  (B)  $\frac{d}{dt} - 2f(0) \cot 0 = 0$  (C)  $\frac{d}{dt} + 2f(0) = 0$  (D) none of these  
(A)  $\frac{d}{dt} + e^{x^2} = C$  (B)  $\frac{x}{2} + e^{x^2} = 0$  (C)  $\frac{x}{2} + e^{x^2} = C$  (D) none of these  
(A)  $\frac{x}{2} + e^{x^2} = C$  (B)  $\frac{x}{2} + e^{x^2} = 0$  (C)  $\frac{x}{2} + e^{x^2} = C$  (D) none of these  
(A)  $\frac{x}{2} + e^{x^2} = C$  (D)  $\frac{x}{2} + e^{x^2} = 0$  (C)  $\frac{x}{2} + e^{x^2} = C$  (D) none of these  
(A)  $\frac{x}{2} + e^{x^2} = C$  (D)  $\frac{x}{2} + e^{x^2} = 0$  (D)  $\frac{2x}{2} \sin y + y^2 \sin x = C$   
(D)  $\frac{2x}{2} \sin y + y^2 \sin x = C$  (D)  $\frac{2x}{2} \sin y + y^2 \sin x = C$   
(D)  $\frac{2x}{2} \sin y + y^2 \sin x = C$  (D)  $\frac{2x}{2} \sin y + y^2 \sin x = C$   
(D)  $\frac{2x}{2} \sin y + y^2 \sin x = C$  (D)  $\frac{2x}{2} \sin y + y^2 \sin x = C$   
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(D)  $\frac{2x}{2} \sin y + y^2 \sin x = C$  (D)  $\frac{2x}{2} \sin y + y^2 \sin x = C$   
(A)  $\frac{y}{2} a(y^2 + x) + y = 1$  is  

# Get Solution of These Packages & Learn by Video Tutorials on www.MathsBySuhag.com (a) $x^2 dy + y(x + y) dx = 0$ , given that y = 1, when x = 1

(b) 
$$\left[x\cos\left(\frac{y}{x}\right)+y\sin\left(\frac{y}{x}\right)\right]y-\left[y\sin\left(\frac{y}{x}\right)-x\cos\left(\frac{y}{x}\right)\right]x\frac{dy}{dx}=0$$

Find the equation of the curve satisfying  $\frac{dy}{dx} = \frac{y^2 - 2xy - x^2}{v^2 + 2xv - x^2}$  and passing through (1, -1).

Find the solution of the differential equation  $\frac{d^3y}{dx^3} = 8 \frac{d^2y}{dx^2}$  satisfying  $y(0) = \frac{1}{8}$ ,  $y_1(0) = 0$  and  $y_2(0) = 1$ .

**Solve** :(i) 
$$(x + 3y^2) \frac{dy}{dx} = y, y > 0$$
 (ii)  $(1 + y + x^2y) dx + (x + x^3) dy = 0$   
(iii)  $\frac{dy}{dx} = y \tan x - 2\sin x$  (iv)  $(1 + x^2) \frac{dy}{dx} + 2xy = \cos x$   
Solve :(i)  $y(x^2y + e^x) dx = e^x dy$  (ii)  $x \frac{dy}{dx} + y = x^2y^4$   
(iii)  $2y \sin x dy + (y^2 \cos x + 2x) dx = 0$   
Solve the following differential equations.  $3 \frac{dy}{dx} + \frac{2y}{x+1} = \frac{x^3}{y^2}$   
Find the curve  $y = f(x)$  where  $f(x) \ge 0$ ,  $f(0) = 0$ , bounding a curvilinear trapezoid with the base  $[0, x]$  whose area area is propostinal to  $(n + 1)^{\text{th}}$  power of  $f(x)$ . It is known that  $f(1) = 1$   
Find the nature of the curve for which the length of the normal at the point P is equal to the radius vector of the  $2x$ 

dv

Find the nature of the curve for which the length of the normal at the point P is equal to the radius vector of the point P.

A particle, P, starts from origin and moves along positive direction of y-axis. Another particle, Q, follows P i.e. 👝 it's velocity is always directed towards P, in such a way that the distance between P and Q remains constant. If Q starts from (2, 0), find the equation of the path traced by Q. Assume that they start moving at the same instant.

Let  $c_1$  and  $c_2$  be two integral curves of the differential equation  $\frac{dy}{dx} = \frac{x^2 - y^2}{x^2 + y^2}$ . A line passing through origin meets  $c_1$  at  $P(x_1, y_1)$  and  $c_2$  at  $Q(x_2, y_2)$ . If  $c_1 : y = f(x)$  and  $c_2 : y = g(x)$  prove that  $f'(x_1) = g'(x_2)$ 

Find the integral curve of the differential equation  $x(1 - xy) \frac{dy}{dx} + y = 0$  which passes through (1, 1/e).

Show that the integral curves of the equation  $(1 - x^2) \frac{dy}{dx} + xy = ax$  are ellipses and hyperbolas, with the centres at the point (0, a) and the axes parallel to the co-ordinate axes, each curve having one constant axis whose length is equal to 2.

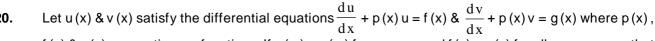
If y<sub>1</sub> & y<sub>2</sub> be solutions of the differential equation  $\frac{dy}{dx}$  + Py = Q, where P & Q are functions of x alone,

 $z = 1 + ae^{-\int \frac{Q}{y_1} dx}$ , 'a' being an arbitrary constant. and  $y_2 = y_1 z$ , then prove that Find the curve for which the sum of the lengths of the tangent and subtangent at any of its point is proportional to the product of the co-ordinates of the point of tangency, the proportionality factor is equal to k.

Find all the curves possessing the following property; the segment of the tangent between the point of

- tangency & the x-axis is bisected at the point of intersection with the y-axis. A curve passing through (1, 0) such that the ratio of the square of the intercept cut by any tangent off the y-axis to the subnormal is equal to the ratio of the product of the co-ordinates of the point of the square of the subnormal terms of the point of the square of the subnormal terms of the point of the square of the subnormal terms of the point of the square of the subnormal terms of the point of the square of the subnormal terms of the point of the square of the subnormal terms of the point of the square of the subnormal terms of the point of the square of the subnormal terms of the point of the square of the subnormal terms of the point of the square of the subnormal terms of the square of the subnormal terms of the square of the subnormal terms of the square of the square of the subnormal terms of the square of the square of the subnormal terms of the square of th tangency to the product of square of the slope of the tangent and the subtangent at the same point.
- Determine all such possible curves. A & B are two separate reservoirs of water. Capacity of reservoir A is double the capacity of reservoir B. Both the reservoirs are filled completely with water , their inlets are closed and then the water is <u>a</u> released simultaneously from both the reservoirs. The rate of flow of water out of each reservoir at any  $\overline{\mathcal{O}}$ instant of time is proportional to the quantity of water in the reservoir at that time. One hour after the owater is released, the quantity of water in reservoir A is 1.5 times the quantity of water in reservoir B.

After how many hours do both the reservoirs have the same quantity of water in reservoir B. A curve y = f(x) passes through the point P (1 ,1). The normal to the curve at P is ; a (y-1) + (x-1) = 0. If the slope of the tangent at any point on the curve is proportional to the ordinate of the point, determine the equation of the curve. Also obtain the area bounded by the y-axis, the curve [IIT - 1996, 5 ] & the normal to the curve at P.



f (x) & g(x) are continuous functions. If  $u(x_1) > v(x_1)$  for some x, and f (x) > g(x) for all x > x\_1, prove that any point (x, y) where  $x > x_1$  does not satisfy the equations y = u(x) & y = v(x).

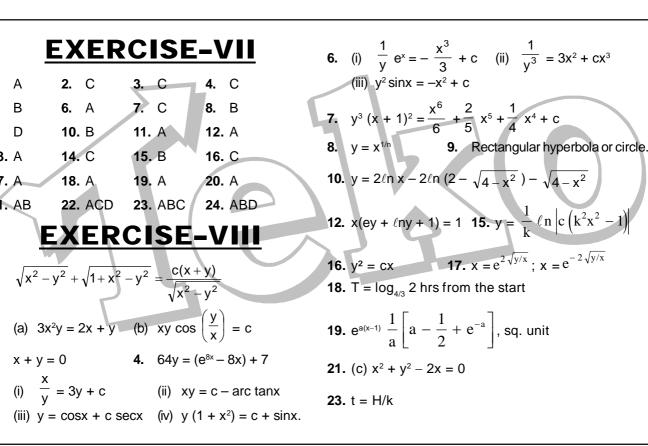
A curve passing through the point (1, 1) has the property that the perpendicular distance of the origin from the normal at any point P of the curve is equal to the distance of P from the x-axis. Determine the 🗟 [IIT - 1999, 10] equation of the curve.

equation of the curve. [IIT - 1999, 10] A country has a food deficit of 10 %. Its population grows continuously at a rate of 3 % per year. Its of annual food production every year is 4 % more than that of the last year. Assuming that the average food requirement per person remains constant, prove that the country will become self-sufficient in

 $\ell n 10 - \ell n 9$ food after 'n' years, where 'n' is the smallest integer bigger than or equal to,  $\ell n (1.04) - 0.03$ 

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 $\ell$  n (1.04) - 0.03 [IIT - 2000 (Mains) 10] An inverted cone of height H and radius R is pointed at bottom. It is filled with a volatile liquid completely. 0 98930 If the rate of evaporation is directly proportional to the surface area of the liquid in contact with air (constant of proportionality k > 0), find the time in which whole liquid evaporates. [IIT - 2003 (Mains) 4]



For 39 Years Que. from IIT-JEE(Advanced) & 15 Years Que. from AIEEE (JEE Main) we distributed a book in class room