- the Complement Of The Event A denoted by  $\overline{A}$  or  $A^c$ .
- site: www.TekoClasses.com & www.MathsBySu over the time of **COMPOUND EVENT**: If A & B are two given events then A $\cap$ B is called COMPOUND EVENT and is denoted by A $\cap$ B or AB or A & B. **MUTUALLY EXCLUSIVE EVENTS**: Two events are said to be **MUTUALLY EXCLUSIVE** (or disjoint or incompatible) if the occurrence of one precludes (rules out) the simultaneous occurrence of the other. If A & B are two mutually exclusive events then P(A & B) = 0.
  - EQUALLY LIKELY EVENTS : Events are said to be EQUALLY LIKELY when each event is as likely to occur as any other event.
  - EXHAUSTIVE EVENTS : Events A,B,C ...... L are said to be EXHAUSTIVE EVENTS if no event outside this set can result as an outcome of an experiment . For example, if A & B are two events defined on a sample space S, then A & B are exhaustive  $\Rightarrow A \cup B = S \Rightarrow P(A \cup B) = 1$ .

(viii) CLASSICAL DEF. OF PROBABILITY : If n represents the total number of equally likely, mutually exclusive and exhaustive outcomes of an experiment and m of them are favourable to the happening of the event A, then the probability of happening of the event A is given by P(A) = m/n.

Note : (1)  $0 \le P(A) \le 1$ 

- $P(A) + P(\overline{A}) = 1$ , Where  $\overline{A} = Not A$ . (2)
- (3) If x cases are favourable to A & y cases are favourable to  $\overline{A}$  then P(A) = and

We say that ODDS IN FAVOUR OF A are x: y & odds against A are y: x

## Comparative study of Equally likely, Mutually Exclusive and Exhaustive events.

×								
<u>ě</u>		Experiment	Events	E/L	M/E	Exhaustive		
≥ E	1.	Throwing of a die	A : throwing an odd face {1, 3, 5} B : throwing a composite face {4,. 6}	No	Yes	No		
ge fro	2.	A ball is drawn from an urn containing 2W, 3R and 4G balls	$E_1$ : getting a W ball $E_2$ : getting a R ball $E_3$ : getting a G ball	No	Yes	Yes		
Packa	3.	Throwing a pair of dice	A : throwing a doublet {11, 22, 33, 44, 55, 66} B : throwing a total of 10 or more {46, 64, 55, 56, 65, 66}	Yes	No	No		
Study	4.	From a well shuffled pack of cards a card is drawn	$E_1$ : getting a heart $E_2$ : getting a spade $E_3$ : getting a diamond $E_4$ : getting a club	Yes	Yes	Yes		
nload	5.	From a well shuffled pack of cards a card is drawn	A = getting a heart B = getting a face card	No	No	No		
≥1	RESULT – 2							
Ó		AUB = A + B = A  or  B	denotes occurence of at least					
$\square \qquad \text{A or B. For 2 events A \& B : (See fig.1)}$								
Ш(	<b>i</b> )	$P(A \cup B) = P(A) + P(B) - P(A \cap B) =$						
Ш		$P(A. \overline{B}) + P(\overline{A}.B) + I$	$P(A.B) = 1 - P(\overline{A} \cdot \overline{B})$					
Ш,	(ii)	Opposite of "atleast	A or B" is niether A nor B					
		i.e. $\overline{A+B} = 1-(A \text{ or } B) = \overline{A} \cap \overline{B}$						

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F	<b>Note that</b> $P(A+B) + P(\overline{A} \cap \overline{B}) = 1.$									
<u>S</u> (	(iii)	If A & B are mutually exclusive then $P(A \cup B) = P(A) + P(B)$ .								
0.0	(iv)	For any two events A & B, P(exactly one of	f A, B occurs)							
ğ		$= P(A \cap \overline{B}) + P(B \cap \overline{A}) = P(A) + P(B) - 2P(A \cap B)$								
h		$= P(A \cup B) - P(A \cap B) = P(A^{c} \cup B^{c}) - P(A^{c} \cap B^{c})$								
<u>က</u> (	( <b>v</b> )	If A & B are any two events $P(A \cap B) = P(A) \cdot P(B/A) = P(B) \cdot P(A/B)$ . Where $P(B/A)$ means								
ഹ		conditional probability of B given A & P(A/B) means conditional probability of A given B. (This can								
hs	( <b>v</b> . <b>i</b> )	be easily seen from the figure) $\mathbf{D} \mathbf{E} \mathbf{M} \mathbf{O} \mathbf{D} \mathbf{C} \mathbf{A} \mathbf{V} \mathbf{S} \mathbf{I} \mathbf{A} \mathbf{W} = \mathbf{I} \mathbf{f} \mathbf{A} \mathbf{g} \mathbf{R}$ are two su	heats of a universal set II then							
ät	(VI)	<b>DE MORGAN'S LAW</b> : - If A & B are two subsets of a universal set U, then (a) $(A \cup B)^c - A^c \supset B^c  \&  (b)  (A \cap B)^c - A^c \cup B^c$								
Σı	vii)	(a) $(A \cap B) = A \cap B$ $\Delta \cup (B \cap C) = (\Delta \cup B) \cap (\Delta \cup C)$ & $\Delta \cap (B \cup C) = (A \cap B) \cup (A \cap C)$								
ξì	DECII									
ξ	NESU.	$E_1 = 3$	$A \rightarrow U$							
á		have (See Fig. 2)	$\left( \begin{array}{c} \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\$							
Ē	<b>(1)</b>	D(A  or  P  or  C) = D(A) + D(P)	$A \cap \overline{B} \cap \overline{C} (A \cap B \cap \overline{C})$							
p,	(1)	$+P(C)-P(A \cap B)-P(B \cap C)-$								
0.0		$P(C \cap A) + P(A \cap B \cap C)$								
ě.	ii)	P(at least two of A.B.C occur) =								
SS		$P(B \cap C) + P(C \cap A) +$								
$\frac{1}{2}$		$P(A \cap B) - 2P(A \cap B \cap C)$	$A \cap C \cap \overline{B} \land C \cap B \cap \overline{A}$							
8	(iii)	P(exactly two of A,B,C occur) =								
<u>ж</u>		$P(B \cap C) + P(C \cap A) $	$\overline{A \cap \overline{B} \cap \overline{C}}$							
Ę.		$P(A \cap B) - 3P(A \cap B \cap C)$	$C(A) B \leftarrow C$							
}(	(iv)	P(exactly one of A,B,C occurs) =	Encl. D. Dr. (A Fig. 2g)							
≶	_	$P(A) + P(B) + P(C) - 2P(B \cap C) - 2P(C \cap A)$	$(A \cap B) + 3P(A \cap B)$							
	NOTE :									
te		If three events A, B and C are pair wise m	utually exclusive then they must be mutually exclusive.							
S		i.e $P(A \cap B) = P(B \cap C) = P(C \cap A) = 0 \Longrightarrow P(A \cap B)$	$A \cap B \cap C$ = 0. However the converse of this is not true.							
١Ģ	RESU	LT - 4								
5		<b>INDEPENDENT EVENTS</b> : Iwo events A & B a of one does not effect the probability of the c	re said to be independent if occurence or non occurence							
	í)	If the occurrence of one event affects the probability of the o	ability of the occurrence of the other event then the events							
fr		are said to be <b>Dependent</b> or <b>Contingent</b> . F	or two independent events							
g	( <b>!!</b> )	A and B : $P(A \cap B) = P(A)$ . P(B). Often this	is taken as the definition of independent events.							
ğ	<b>(II)</b>	I hree events A, B & C are independent if & $P(\Delta \cap B) - P(\Delta) P(B) \rightarrow P(B)$	only if all the following conditions hold; D(C) = P(B) = P(C)							
ð		$P(C \cap A) = P(C) \cdot P(A)$ , $P(A)$	$\neg B \cap C) = P(A) \cdot P(B) \cdot P(C)$							
л П		i.e. they must be pairwise as well as mut	ually independent .							
>		Similarly for n events $A_1, A_2, A_3, \dots, A_n$ to	b be independent, the number of these conditions is equal							
Ъ	iii)	The probability of getting exactly r success $\frac{1}{2}$	in n independent trials is given by							
<u>5</u> `	<b>"</b>	$P(r) = {}^{n}C_{p} p^{r} q^{n-r}$ where : $p = pro$	bability of success in a single trial.							
Q		q = probability of failure in a single trial. note : p + q = 1.								
oa		Note : Independent events are not in general mutually exclusive & vice versa.								
Ē		can be used when the events are taken from a	lifferent experiments							
≥.	RESU	$TT = 5 \cdot BAVE'S THEOREM OR TOTAL PE$	ROBABILITY THEOREM .							
ŏ.		If an event A can occur only with one of the	n mutually exclusive and exhaustive events $B_1, B_2, \dots, B_n$							
Щ		$(A/B_n)$ are known then,								
Ш		$P(B/A) = \frac{P(B_i).P(A/B_i)}{P(B_i)}$								
Ë		$\sum_{n=1}^{n} P(\mathbf{R}) P(\mathbf{A}/\mathbf{R})$								
		$\sum_{i=1}^{n} \mathbf{I} \left( \mathbf{D}_{i} \right) \cdot \mathbf{I} \left( \mathbf{A} / \mathbf{D}_{i} \right)$								
	Suc	cassful Boonlo Bonlaco the words like: "wish" "f	ry" & "should" with "I Will" Ineffective Reanle don't							

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The following statements are axiomatic:

If a point is taken at random on a given staright line AB, the chance that it falls on a particular (i) Successful People Replace the words like; "wish", "try" & "should" with "I Will". Ineffective People don't.

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E(ii)	segment PQ of the line is PQ/AB. If a point is taken at random on the area S which includes an area $\sigma$ , the chance that the point
0.0 0	EXERCISE-1
Q.1	Let a die be weighted so that the probability of a number appearing when the die is tossed is proportional
N N	to that number. Find the probability that, (i) An even or a prime number appears (ii) An odd prime number appears $\Im$
B A	<ul> <li>(ii) An even composite number appears</li> <li>(ii) An odd composite number appears</li> <li>(iv) An odd composite number appears.</li> </ul>
و Q.2	numbers are selected at random, one at a time, from the two digit numbers 00, 01, 02,, 99 with greplacement. An event E occurs if & only if the product of the two digits of a selected number is 18.
N Aa	If four numbers are selected, find the probability that the event E occurs at least 3 times.
<u>,</u> Q.3	that the word 'ASH' will form if:
<b>≤</b> (i)	the three cards are drawn one by one & placed on the table in the same order that they are drawn.
<b>න්</b> Q.4	There are 2 groups of subjects one of which consists of 5 science subjects & 3 engg. subjects & other 8
ШO	is selected at random from first group, otherwise the subject is selected from 2 <sup>nd</sup> group. Find the
Ŭ ØO 5	probability that an engg. subject is selected.
9.9 9 9	In a building programme the event that all the materials will be delivered at the correct time is M, and the
las	event that the building programme will be completed on time is F. Given that $P(M) = 0.8$ and $\Im$ $P(M \cap F) = 0.65$ , find $P(F/M)$ . If $P(F) = 0.7$ , find the probability that the building programme will $\Im$
$\overline{O}$	be completed on time if all the materials are not delivered at the correct time .
	Assuming that a dead heat is impossible, find the chance that one of them wins the race.
⊢Q.8 ≥	A covered basket of flowers has some lilies and roses. In search of rose, Sweety and Shweta alternately 5 nick up a flower from the basket but puts it back if it is not a rose. Sweety is 3 times more likely to be the
$\mathbf{x}$	first one to pick a rose. If sweety begin this 'rose hunt' and if there are 60 lilies in the basket, find the $\frac{1}{\overline{\alpha}}$
>0.9	number of roses in the basket. Least number of times must a fair die be tossed in order to have a probability of at least $91/216$ , $\frac{2}{2}$
	of getting at least one six. Suppose the probability for $A$ to win a game against B is 0.4. If A has an option of playing either a $\widehat{a}$
SQ.10	"BEST OF THREE GAMES" of a "BEST OF 5 GAMES" match against B, which option should A choose $\mathcal{O}$
¥ <sub>0.11</sub>	so that the probability of his winning the match is higher? (No game ends in a draw). $\checkmark$ A room has three electric lamps. From a collection of 10 electric bulbs of which 6 are good 3 are $\dot{\sigma}$
E	selected at random & put in the lamps. Find the probability that the room is lighted.
<u></u>	If four bombs are dropped, what is the probability that it is destroyed, if the chance of a bomb hitting the
$\mathbf{D}_{0}$	target is 0.4. The chance of one event happening is the square of the chance of a $2^{nd}$ event, but odds against the first $\mathbf{X}$
YO YO	are the cubes of the odds against the $2^{nd}$ . Find the chances of each. (assume that both events are neither $\alpha$
0.14	A box contains 5 radio tubes of which 2 are defective. The tubes are tested one after the other until the
र्वे	2 defective tubes are discovered. Find the probability that the process stopped on the
Stu	tube is non defective.
ע <sub>Q.15</sub> ס	Anand plays with Karpov 3 games of chess. The probability that he wins a game is 0.5, looses with $\Im$
	atleast two games.
	of hitting the plane at first, second, third & fourth shots are 0.4, 0.3, 0.2 & 0.1 respectively. What is the
$\overset{o}{O}_{0.17}$	probability that the gun hits the plane.
— с.17	If more than 2 articles in this batch are defective, the whole batch is rejected Find the probability that $\stackrel{\circ}{\vdash}$
	the batch will be rejected. Given $P(A \cup B) = 5/6 \cdot P(AB) = 1/3 \cdot P(\overline{B}) = 1/2$ . Determine $P(A \cup B \cap D(B)$ . Hence show that the
	Given $\Gamma(X \supset D) = J(D) + \Gamma(D) = 1/2$ , $\Gamma(D) = 1/2$ . Determine $\Gamma(A) \otimes \Gamma(D)$ . Hence show that the

- If more than 2 articles in this batch are defective, the whole batch is rejected Find the probability that  $\stackrel{\circ}{\vdash}$ the batch will be rejected.
  - Given  $P(A \cup B) = 5/6$ ; P(AB) = 1/3;  $P(\overline{B}) = 1/2$ . Determine P(A) & P(B). Hence show that the events A & B are independent.



- Get Solution of These Packages & Learn by Video Tutorials on www.MathsBySuhag.com 1.0. Find the probability of destroying the target in three shots.
- In a game of chance each player throws two unbiased dice and scores the difference between the larger and smaller number which arise. Two players compete and one or the other wins if and only if he scores at least 4 more than his opponent. Find the probability that neither player wins.
- - IS TOXIC'' be denoted by S. Let P(H) = a,  $P(S/H) = P(\overline{S}/\overline{H}) = 1 a$ . Then show that the probability that the drug is not toxic given that the chemical test reveals that it is toxic, is free from 'a'.
- A plane is landing. If the weather is favourable, the pilot landing the plane can see the runway. In this case the probability of a safe landing is  $p_1$ . If there is a low cloud ceiling, the pilot has to make a blind landing by instruments. The reliability (the probability of failure free functioning) of the instruments needed for a blind landing is P. If the blind landing instruments function normally, the plane makes a safe landing with the same  $\frac{1}{80}$  probability  $p_1$  as in the case of a visual landing. If the blind landing instruments fail, then the pilot may make  $\frac{1}{80}$  a safe landing with probability  $p_2 < p_1$ . Compute the probability of a safe landing if it is known that in K percent of the cases there is a low cloud ceiling. Also find the probability that the pilot used the blind landing S instrument, if the plane landed safely.
- FREE Download Study Package from website: www.TekoClasses.com & www.MathsBySuhag.com <sup>6,7</sup> <sup>6,7</sup> <sup>6,9</sup> <sup>7,0</sup> <sup>6,0</sup> <sup>6,0</sup> <sup>6,0</sup> <sup>6,0</sup> <sup>6,0</sup> <sup>6,0</sup> <sup>6,0</sup> <sup>7,0</sup> <sup>6,0</sup> <sup>7,0</sup> <sup>6,0</sup> <sup>7,0</sup> <sup>7,1</sup> A train consists of n carriages, each of which may have a defect with probability p. All the carriages are inspected, independently of one another, by two inspectors; the first detects defects (if any) with  $\circ$ probability  $p_1$ , & the second with probability  $p_2$ . If none of the carriages is found to have a defect, the train departs. Find the probability of the event; "THE TRAIN DEPARTS WITH ATLEAST ONE **DEFECTIVE CARRIAGE** ".
  - A is a set containing n distinct elements. A non-zero subset P of A is chosen at random. The set A is reconstructed by replacing the elements of P. A non-zero subset Q of A is again chosen at random. Find the probability that P & Q have no common elements.
  - In a multiple choice question there are five alternative answers of which one or more than one is correct. A candidate will get marks on the question only if he ticks the correct answers. The candidate ticks the answers at random. If the probability of the candidate getting marks on the question is to be greater than or equal to 1/3 find the least number of chances he should be allowed.
  - n people are asked a question successively in a random order & exactly 2 of the n people know the answer:
    - If n > 5, find the probability that the first four of those asked do not know the answer.
    - Show that the probability that the r<sup>th</sup> person asked is the first person to know the answer is : 2(n-r)

if 1 < r < n. n(n-1)

- A box contains three coins two of them are fair and one two headed. A coin is selected at random and 😒 tossed. If the head appears the coin is tossed again, if a tail appears, then another coin is selected from  $\dot{\alpha}$ the remaining coins and tossed.
- Find the probability that head appears twice.
- If the same coin is tossed twice, find the probability that it is two headed coin.
- Find the probability that tail appears twice.
- The ratio of the number of trucks along a highway, on which a petrol pump is located, to the number of cars running along the same highway is 3 : 2. It is known that an average of one truck in thirty trucks and  $\vec{r}$ two cars in fifty cars stop at the petrol pump to be filled up with the fuel. If a vehicle stops at the petrol pump to be filled up with the fuel, find the probability that it is a car. A batch of fifty radio sets was purchased from three different companies A, B and C. Eighteen of them
- were manufactured by A, twenty of them by B and the rest were manufactured by C.

 $_{-1}$   $_{-1$ Successful People Replace the words like; "wish", "try" & "should" with "I Will". Ineffective People don't.



Get Solution of These Packages & Learn by Video Tutorials on www.MathsBySuhag.com (A) P (E|F) + P(E|F) = 1 (B) P (E|F) + P(E|F) = 1 (C) P (E|F) + P(E|F) = 1 (D) P (E|F) + P(E|F) = 1 (C) P (E|F) + P(E|F) = 1 (D) P (E|F) + P(E|F) = 1 (C) P (E|F) + P(E|F) = 1 (D) P (E|F) + P(E|F) = 1 (C) P (E|F) + P(E|F) = 1 (D) P (E|F) + P(E|F) + 2 (D) P (E|F) + 2 (D) Get Solution of These Packages & Learn by Video Tutorials on www.MathsBySuhag.com his target whereas C does not. [JEE' 2003, Mains-2 + 2 out of 60] L Q.14(a) Three distinct numbers are selected from first 100 natural numbers. The probability that all the three numbers are divisible by 2 and 3 is Successful People Replace the words like; "wish", "try" & "should" with "I Will". Ineffective People don't.

(A)  $\frac{4}{2\xi}$ (b) If A and defined (c) A bag of which a drawn (c) A bag of the composition of the composi (A)  $\frac{1}{25}$ (B)  $\frac{1}{35}$ (C)  $\overline{55}$ (D)  $\frac{1155}{1155}$ (b) If A and B are independent events, prove that  $P(A \cup B) \cdot P(A' \cap B') \le P(C)$ , where C is an event defined that exactly one of A or B occurs. (c) A bag contains 12 red balls and 6 white balls. Six balls are drawn one by one without replacement of 😓 which at least 4 balls are white. Find the probability that in the next two draws exactly one white ball is drawn (leave the answer in terms of  ${}^{n}C_{r}$ ). [JEE 2004, 3+2+4]page 28 15(a) A six faced fair dice is thrown until 1 comes, then the probability that 1 comes in even number of trials (A) 5/11 (B) 5/6 (C) 6/11 (D) 1/6 (b) A person goes to office either by car, scooter, bus or train probability of which being  $\frac{1}{7}, \frac{3}{7}, \frac{2}{7}$ 98930 58881. respectively. Probability that he reaches office late, if he takes car, scooter, bus or train is  $\frac{2}{9}$ ,  $\frac{1}{9}$ ,  $\frac{4}{9}$  and  $\frac{1}{9}$  respectively. Given that he reached office in time, then what is the probability that he travelled by a car. [JEE 2005 (Mains), 2]  $\begin{array}{c} \text{Comprehension (3 questions)} \\ \text{There are $n$ urns each containing $n$ + 1 balls such that the $i^{th}$ urn contains $i$ white balls and (n + 1 - i) red balls. Let $u_{b}$ be the event of selecting $n^{th}$ urn, $i = 1, 2, 3, ..., $n$ and $w$ denotes the event of getting $a$ white balls. Let $u_{b}$ the event of selecting $n^{th}$ urn, $i = 1, 2, 3, ..., $n$ and $w$ denotes the event of getting $a$ white balls and (n + 1 - i) red balls. Let $u_{b}$ the event of selecting $n^{th}$ urn, $i = 1, 2, 3, ..., $n$ and $w$ denotes the event of getting $a$ white balls and (n + 1 - i) red balls. Let $u_{b}$ the event of selecting $n^{th}$ urn, $i = 1, 2, 3, ..., $n$ and $w$ denotes the event of getting $a$ white balls and (n + 1 - i) red balls. Let $u_{b}$ the event of selecting $n^{th}$ urn, $i = 1, 2, 3, ..., $n$ and $w$ denotes the event of getting $a$ white balls and (n + 1 - i) red balls. Let $u_{b}$ the event of selecting $n^{th}$ urn, $i = 1, 2, 3, ..., $n$ and $w$ denotes the event of getting $a$ white balls and (n + 1 - i) red balls. Let $u_{b}$ the event of selecting $n^{th}$ urn, $i = 1, 2, 3, ..., $n$ and $w$ denotes the event of getting $a$ white balls and (n + 1 - i) red balls. Let $u_{b}$ the event of selecting $n^{th}$ urn, $i = 1, 2, 3, ..., $n$ and $w$ denotes the event of getting $a$ white balls and (n + 1 - i) red balls. Let $u_{b}$ the event of choosing even numbered $u^{th}$ (D) 1/4 (D$ Õ **Comprehension (3 questions)** Q.16(a) If  $P(u_i) \propto i$  where i = 1, 2, 3, ..., n then Lim P(w) is equal to (b) If  $P(u_i) = c$ , where c is a constant then  $P(u_n/w)$  is equal to (c) If *n* is even and E denotes the event of choosing even numbered urn  $(P(u_i) =$ (i)  $\frac{20}{21}$  (ii)  $\frac{8}{21}$  (iii)  $\frac{10}{21}$  (iv) 0 **Q 10.** best of 3 games **びQ 14. (i)** 1/10, (ii) 3/10, (iii) 2/3 Q 17. 19/42 Q 20. 407/5' Q 20. 407/576 Q 23. 101/1326 **Q 26.**  $P_1 = 1/2$  ,  $P_2 = 3/4$  $\square$  Q25. Independent in (a) and not independent in (b) **Q 28.**  $\left(\frac{5}{6} + \frac{1}{6}\right)^{36}$ **Q 27.**  $(1-p)^{n-1}$ . [ $p_o(1-p) + np(1-p_0)$ ]

## **EXERCISE-4**

**Boy Part :** (A) Only one correct option Of 1. If A, B, C are 3 events, then the (A)  $P(A \cap B) + P(B \cap C) = (B) P(A \cap B) + P(B \cap C) = (D)$  (D) none of these In a series of 3 independent probability of 3 successes. The east two urns. There are second urn. One ball is tak drawing a white ball from the (A)  $\frac{pm + (p + 1)n}{(m + n)(p + q + 1)}$  (B) Solution (A)  $\frac{pm + (p + 1)n}{(m + n)(p + q + 1)}$  (B) Solution (A)  $\frac{12}{17}$  (B) Solution (A)  $\frac{12}{19}$  (B) Solution (A)  $\frac{12}{19}$  (B) Solution (A)  $\frac{12}{19}$  (B) Solution (A)  $\frac{12}{17}$  (B) Solution (A)  $\frac{12}{17}$  (B) Solution (A)  $\frac{12}{17}$  (B) Solution (A)  $\frac{12}{17}$  (B) Solution (B) Solution (A)  $\frac{12}{17}$  (B) Solution (C) If A, B, C are 3 events, then the probability that exactly 2 of them occur is given by:  $P(A \cap B) + P(B \cap C) + P(C \cap A) - 2P(A \cap B \cap C)$  $P(A \cap B) + P(B \cap C) + P(C \cap A) - 3P(A \cap B \cap C)$ page 30 of 37  $P(A) + P(B) + P(C) - P(A \cap B) - P(B \cap C) - P(C \cap A) + P(A \cap B \cap C)$ In a series of 3 independent trials the probability of exactly 2 success is 12 times as large as the probability of 3 successes. The probability of a success in each trial is: (B) 2/5 (C) 3/5 (D) 4/5 There are two urns. There are m white & n black balls in the first urn and p white & q black balls in the second urn. One ball is taken from the first urn & placed into the second. Now, the probability of drawing a white ball from the second urn is: (A)  $\frac{pm + (p + 1)n}{(m + n)(p + q + 1)}$  (B)  $\frac{(p + 1)m + pn}{(m + n)(p + q + 1)}$  (C)  $\frac{qm + (q + 1)n}{(m + n)(p + q + 1)}$  (D)  $\frac{(q + 1)m + qn}{(m + n)(p + q + 1)}$  (D)  $\frac{($ event 'ball drawn is from Box-I, if it is red'. 0 (D)  $\frac{3}{5}$ 17 (C) <u>20</u> 903 9037779, A local post office is to send M telegrams which are distributed at random over N communication channels, (N > M). Each telegram is sent over any channel with equal probability. Chance that not more than one telegram will be sent over each channel is: <sup>N</sup>C<sub>M</sub> . M ! <sup>N</sup>C<sub>M</sub> . N ! <u>°С<sub>м</sub> .</u> N ! (C) 1 (D) 1 – M<sup>N</sup> NM M<sup>N</sup> 0 A mapping is selected at random from all the mappings defined on the set A consisting of three distinct elements. The probability that the mapping selected is one to one is: **Bhopal Phone** (A) 1/9 (B) 1/3 (C) 1/4 (D) 2/3 A bag contains 7 tickets marked with the numbers 0, 1, 2, 3, 4, 5, 6 respectively. A ticket is drawn & (B) 149/2401 (C) 3/49 (D) none À biased coin with probàbility p, 0 < p < 1 of heàdś is tossed until a head áppears for the first time. If the probability that the number of tosses required is even is 2/5, then p equals (C) 2/5 (B) 2/3 (D) 3/5 If 4 whole numbers taken at random are multiplied together, then the chance that the last digit in the ភ (A) 16/625 (B) 4/125 (C) 8/81 (D) none A letter is known to have come either from "KRISHNAGIRI" or "DHARMAPURI". On the post mark only (B) 4/125 (C) 8/81 the two consecutive letters "RI" are visible. Then the chance that it came from Krishnagiri is: ė (C) 9/14 (B) 2/3 (D) none Ś are the probabilities of three mutually exclusive events then the set of all Classes, Maths : Suhag R. Kariya  $\frac{1}{3}, \frac{1}{2}$ (D) 3'3 4 Let p be the probability that a man aged x years will die in a year time. The probability that out of 'n men A<sub>1</sub>, A<sub>2</sub>, A<sub>3</sub>,...., A<sub>n</sub> each aged 'x' years. A<sub>1</sub> will die & will be the first to die is: (C)  $\frac{p(1-p)^{n-1}}{p}$  $1 - (1 - p)^n$ 5 girls and 10 boys sit at random in a row having 15 chairs numbered as 1 to 15, then the probability that end seats are occupied by the girls and between any two girls an odd number of boys sit is:  $10 \times 10! \times 5!$  $20 \times 10! \times 30$  $10 \times 10! \times 5!$ 15! 151 Two dice are rolled simultaneously. The probability that the sum of the two numbers on the top faces (A) 1/6 (B) 1/12 (C) 1/18 (D) none Q There are 4 urns. The first urn contains 1 white & 1 black ball, the second urn contains 2 white & 3 do black balls, the third urn contains 3 white & 5 black balls & the fourth urn contains 4 white & 7 black H balls. The selection of each urn is not equally likely. The probability of selecting ith urn (i = 1, 2, 3, 4). If we randomly select one of the urns & draw a ball, then the probability of ball being Successful People Replace the words like; "wish", "try" & "should" with "I Will". Ineffective People don't.

Get Solution of These Packages & Learn by Video Tutorials on www.MathsBySuhag.com white is 8 (D) none of these 73 2/3rd of the students in a class are boys & the rest girls. It is known that probability of a girl getting a first class is 0.25 & that of a boy is 0.28. The probability that a student chosen at random will get a first page 31 of 37 (C) 0.27 (D) 0.275 One urn is chosen at random and a ball is drawn and its colour is noted and replaced back to the urn. Again a ball is drawn from the same urn, colour is noted and replaced. The process is repeated 4 times and as a result one ball of white colour and 3 of black colour are noted. Find the probability the chosen 98930 5888 25 79 (C) (D) 287 192 The sides of a rectangle are chosen at random, each less than 10 cm, all such lengths being equally likely. The chance that the diagonal of the rectangle is less than 10 cm is (C) π/4 (D) π/8 The sum of two positive quantities is equal to 2n. The probability that their product is not less than 0 Bhopal Phone : 0 903 9037779, (C) (D) none of these 4 The probability that 4<sup>th</sup> power of a positive integer ends in the digit 6 is: (C) 25 % (D) 40 % Posteriory probability of the occurrance of the event 'The coin turns head and the die turns up an odd 37 47 (C) (D) 200 300 (C) (D) 7 7 For the three events A, B & C, P(exactly one of the events A or B occurs) = P(exactly one of the events B or C occurs) = P(exactly one of the events C or A occurs) = p & P (all the three events occur simultaneously) =  $p^2$  where 0 . Then the probability of at least one of the three events A, B &[IIT -1996] Sir), I p + 3p 3p + 2p (C) (D) Ч. In throwing a die let A be the event 'coming up of an odd number', B be the event 'coming up of an even c number', Č be the event 'coming up of a number  $\geq$  4' and D be the event 'coming up of a number < 3'. ώ. Teko Classes, Maths : Suhag R. Kariya A and C are mutually exclusive and exhautive (B) (D) B, C and D form an exhautive system Let 0 < P(A) < 1, 0 < P(B) < 1 &  $P(A \cup B) = P(A) + P(B) - P(A)$ . P(B), then:  $(\dot{B}) P(\dot{A}^{c'} \cup B^{c}) = P(\dot{A}^{c'}) + P(B^{c})$ (D) P(A/B) = P(A)For any two events A & B defined on a sample space,  $P(B) \neq 0$  is always true if A & B are independent if A & B are disjoint If A, B & C are three events, then the probability that none of them occurs is given by: + P(B) +  $P(C) - P(A \cap B) - P(B \cap C) - P(A \cap C) + P(A \cap B \cap C)$  $- P(B) - P(C) + P(A \cap B) + P(B \cap C) + P(C \cap A) - P(A \cap B \cap C)$  $P(\overline{A} \cup \overline{B} \cup \overline{C}) - P(A) - P(B) - P(C) + P(A \cap B) + P(B \cap C) + P(C \cap A)$ R LL 28. A student appears for tests I, II & III. The student is successful if he passes either in tests I & II or tests I & III. The probabilities of the student passing in the tests I, II & III are p, q &

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E		(A) $p = 1$ , $q = 0$ (B) $p = 2/3$ , $q = 1/2$ (C) $p = 3/5$ , $q = 2/3$ (D) there are infinitely many values of $p \& q$	
S:	29.	If the integers m and n are chosen at random between 1 and 100, then the probability that a number of the formation $\frac{1}{2}$	
ag		(A) 1/4 (B) 1/7 (C) 1/8 (D) 1/49	
η			of 3'
Ś		LALINGIGE-5	32 (
S. B.	1.	A letter is known to have come either from London or Clifton; on the postmark only the two consecutive letters ON are legible: what is the chance that it came from London?	age
Ę	2.	A speaks the truth 3 out of 4 times, and B 5 out of 6 times; what is the probability that they will contradict each other in starting the same fact?	ä
Ž;	3.	A pair of dice is thrown 5 times. Find the mean and variance of the probability distribution of appearance	81.
Ś₄	4.	If on a straight line 10 cm. two length of 6 cm and 4 cm are measured at random, find the probability	588
Š:	5.	that their common part does not exceed 3 cms. Let p be the probability that a man aged x years will die in a year time. Find the probability that out of	30 5
ω.	3	'n' men A <sub>1</sub> , A <sub>2</sub> , A <sub>3</sub> ,, A <sub>n</sub> each aged 'x' years. A <sub>1</sub> will die & will be the second to die.	88
E.	7	exactly 15 placed are still occupied. Find the probability that both the neighbouring places are empty.	0
S,		or unless the coin has been tossed for a maximum of five times. If for each head he wins a rupee and	79,
es.	3.	for each tail he looses a rupee, then find the probability that the gambler is ruined. Mr. Dupont is a professional wine taster. When given a French wine, he will identify it with probability 0.9	277
SS		correctly as French, and will mistake it for a Californian wine with probability 0.1. When given a Californian wine, he will identify it with probability 0.8 correctly as Californian, and will mistake it for a French wine with	06
<u>Cla</u>		probability 0.2. Suppose that Mr. Dupont is given ten unlabelled glasses of wine, three with French and seven with Californian wines. He randomly nicks a glass tries the wine and solemply says "French". Find the	903
<u>Š</u>	<b>`</b>	probability that the wine tasted was Californian.	0
Ţē,	9.	an ten thats of an experiment, if the probability of getting 4 successes is maximum, then show that	ne
' <b>≥</b>		probability of failure in each trial can be equal to $\frac{1}{5}$ .	<sup>o</sup> ho
Š	10.	happening of the variable in 10 trials of the experiment.	alF
	11.	In a Nigerian hotel, among the english speaking people 40% are English & 60% Americans. The English & American spellings are "Rigour" & "Rigor" respectively. An English speaking person in the hotel	hop
ite		writes this word. A letter from this word is chosen at random & found to be a vowel. Find the probability that the writer is an Englishman	Ë B
Śģ	12.	There is a group of k targets, each of which independently of the other targets, can be detected by a radar units detects the targets independently of other units	ŝ
Me Me		Find the probability that not all the targets in the group will be detected.	×.
Ē	13.	2 positive real numbers x and y satisfy $x \le 1$ and $y \le 1$ are chosen at random. Find the probability that	с С
fro		$x + y \le 1$ , given that $x^2 + y^2 \ge \frac{1}{4}$ .	a (9
ge	14.	I here are two lots of identical articles with different amounts of standard & defective articles. I here are N articles in the first lot, n of which are defective & M articles in the second lot, m of which are	ariy
kaj		defective. K articles are selected from the first lot & L articles from the second & a new lot results. Find the probability that an article selected at random from the new lot is defective.	× ×
acl	15.	The odds that a book will be favorably reviewed by three independent crities are 5 to 2, 4 to 3, and 3 to 4 respectively what is the probability that of the three reviews a majority will be favourable?	зg F
Ū,	16.	Find the chance of throwing 10 exactly in one throw with 3 dice.	iuha
þ	17.	If 12 tickets numbered 0, 1, 2,11 are placed in a bag, and three are drawn out, show that the chance	S 
S		that the sum of the numbers on them is equal to 12 is $\frac{3n}{(6n-1)(6n-2)} = \frac{3}{55}$	aths
ğ	18.	A man has 10 coins and one of them is known to have two heads. He takes one at random and tosses it	ŝ
<u>lo</u>	19.	A purse contains five coins, each of which may be a rupees coin or a 50 ps coin ; two are drawn and found	ses
N N	20.	To be shillings : find the probable value of the remaining coins. One of a pack of 52 cards has been lost; from the remainder of the pack two cards are drawn and are found	Clas
$\mathbf{\tilde{c}}$		to be spades; find the chance that the missing card is a spade.	000
Щ	21.	A, B are two inaccurate arithmeticians whose chance of solving a given question correctly are $\frac{1}{8}$ and $\frac{1}{12}$	Te
Ц Ц Ц		respectively; if they obtain the same result, and if it is 1000 to 1 against their making the same mistake, find the chance that the result is correct.	
Шź	22.	If n integers taken at random are multiplied together, show that the chance that the last digit of the product	

Get Solution of These Packages & Learn by Video Tutorials on www.MathsBySuhag.com is 1, 3, 7, or 9 is  $\frac{2^n}{5^n}$ ; the chance of its being 2, 4, 6 or 8 is  $\frac{4^n - 2^n}{5^n}$ ; of its being 5 is  $\frac{5^n - 4^n}{10^n}$ ; and of its being 5 is  $\frac{5^n - 4^n}{10^n}$ ; 0 is  $\frac{10^n - 8^n - 5^n + 4^n}{10^n}$ A player to see a coin and is to score one point for every head and 2 points if every tail turned up. He is to play until he reaches 'n'. If  $p_n$  is the chance of obtaining exactly 'n' crores, find  $p_n$  for  $\mathbf{E}$ 33 n = 1, 2, 3, 4. Also show that  $p_n = \frac{1}{2} (p_{n-1} + p_{n-2})$ . page. A lot contains 50 defective & 50 non defective bulbs. Two bulbs are drawn at random, one at a time, with replacement. The events A, B, C are defined as: [IIT - 1992] B = { the second bulb is non defective} Determine whether (i) A,B,C are pair wise independent (ii) A,B,C are independent Eight players P<sub>1</sub>, P<sub>2</sub>, P<sub>3</sub>,...,P<sub>8</sub> play a knock-out tournament. It is known that whenever the players P and P play, the player P will win if i < j. Assuming that the players are paired at random in each provide the probability that the players P reaches the final. [IIT - 1999] A box contains N coins, m of which are fair and the rest are biased. The probability of getting a head when a fair coin is tossed is 1/2, while it is 2/3 when a biased coin is tossed. A coin is drawn from the box at random and is tossed twice. The first time it shows head and the second time it shows tail. What is the probability that the coin drawn is foir? A = { the first bulb is defective } ; What is the probability that the coin drawn is fair? [IIT - 2002] Q A person has to go through three successive tests. Probability of his passing first exam is P. Probability of passing successive test is P or P/2 according as he passed the last test or not. He is selected if he 37 passes atleast two tests. Find the probability of his selection. [IIT - 2003] Prove that P(A U B) P  $(\overline{A} \cap \overline{B}) \leq P(C)$  where A and B are independent events and P(C) is the probability of  $\mathcal{B}$ exactly one of A or B occurs. [IIT - 2004] A person goes to office either by car, scooter, bus or train, the probability of which being B exactly one of A or B occurs. 0 respectively. Probability that he reaches office late, if he takes car, scooter, bus or Teko Classes, Maths : Suhag R. Kariya (S. R. K. Sir), Bhopal Phone :  $\frac{1}{9}$  and  $\frac{1}{9}$  respectively. Given that he reached office in time, then what is the probability [IIT - 2005] he travelled by a car EXERCISE-5 SF-4 5. 6. B 3. В 7. 12  $\frac{5}{6}$ , variance =  $\frac{25}{36}$ mean = 14. A Α 10. C 11. B 12. D Α 13. 18. C 16. C 17. A 19. B 20. D 21. B  $[1 - (1 - p)^n - np (1 - p)^{n-1}]$ 23. A 24. AC 25. CD 26. AC 27. CD 29. AD **10.** 3 **11.** 6 92  $\frac{8-\pi}{16-\pi}$  **14.**  $\frac{\text{KnM} + \text{LmN}}{\text{MN}(\text{K} + \text{L})}$ 13. **12.**  $1 - \{1 - (1 - p)^m\}^k$ 15. 209/343 16. 1/5 18. (32/41) 19. 2.25 Rs 20. 11/50 21. (13/14) **23.**  $p_1 = \frac{1}{2}, p_2 = \frac{3}{4}, p_3 = \frac{5}{8}, p_4 = \frac{11}{16}$ 24. (i) A, B, C are pairwise independent (ii) A, B, C are not independent 9 m 27. 2 P<sup>2</sup> - P<sup>3</sup> 25. 4/35 26. **29.** 1/7 8 N + m