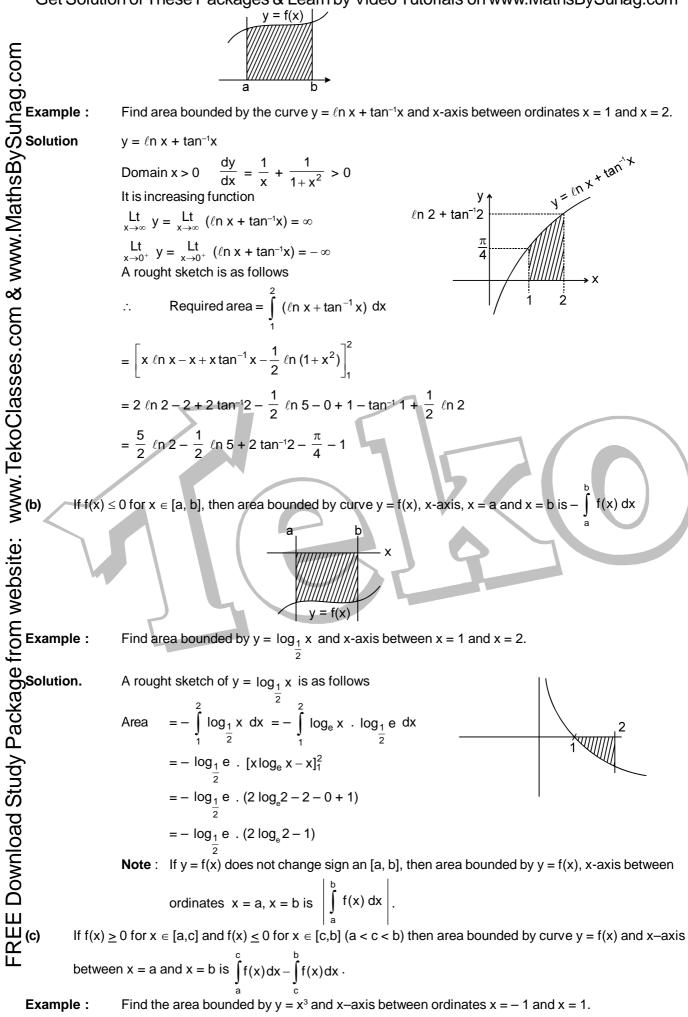
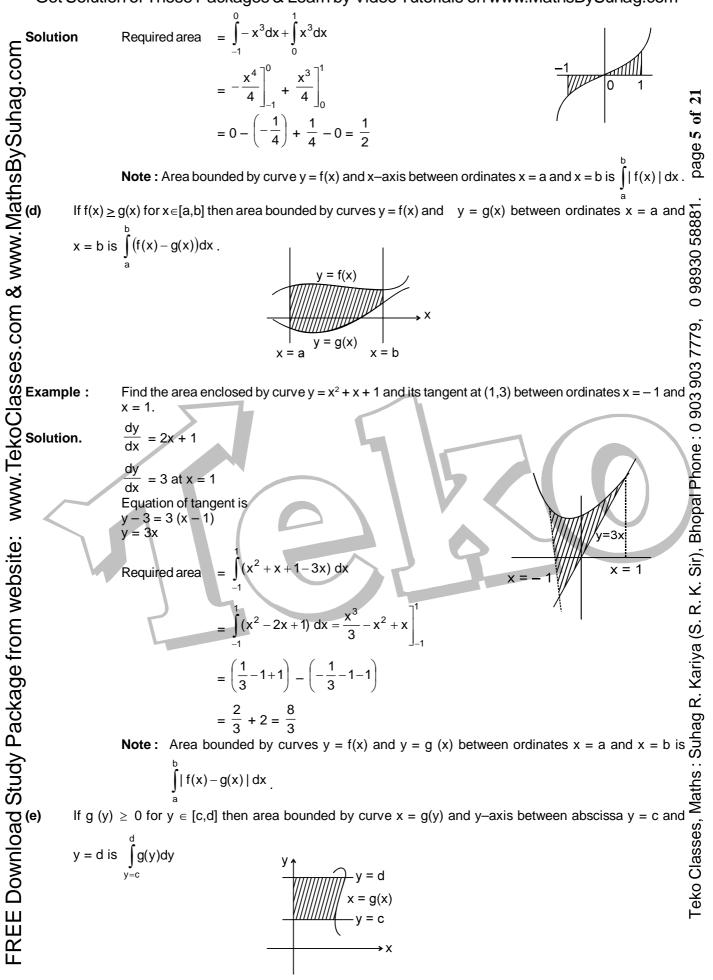
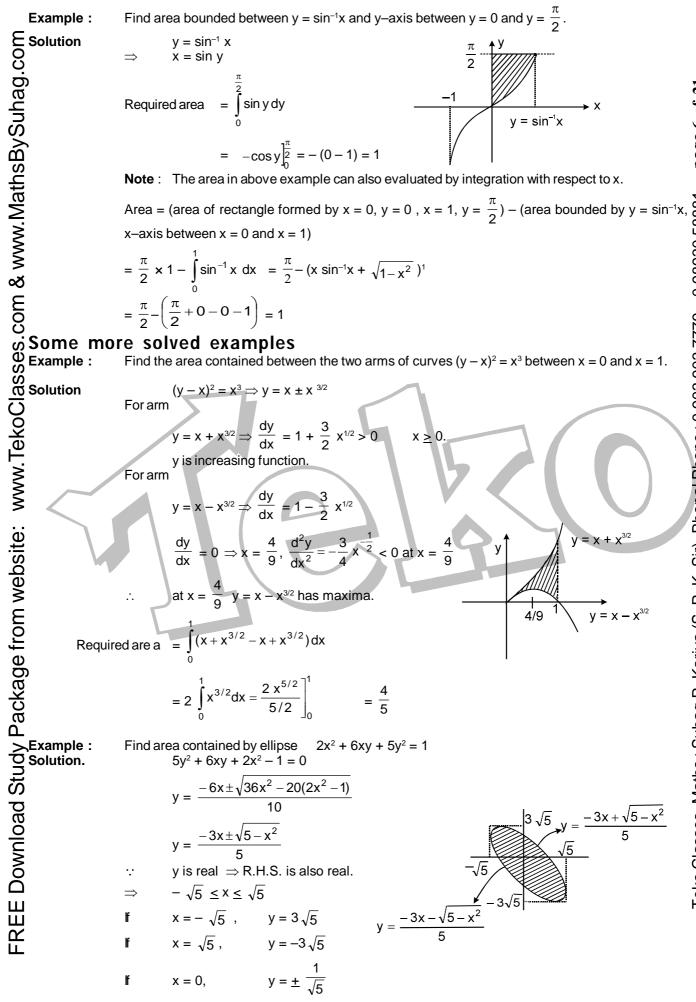


Find  $\frac{dy}{dx}$  and equate it to zero to find the points on the curve where you have horizontal tangents. (c) (i) (ii) (iii) (iii)) (iii) (iii) (iii)) (ii)) (ii)) (ii)) (ii)) (ii)) (ii)) (ii)) ( Examine if possible the intervals when f (x) is increasing or decreasing. 5 Examine what happens to 'y' when  $x \to \infty$  or  $x \to -\infty$ . of Asymptotes : Asymptoto(s) is (are) line (s) whose distance from the curve tends to zero as point on curve moves towards infinity along branch of curve. If  $\underset{x \to a}{\overset{Lt}{\longrightarrow}} f(x) = \infty$  or  $\underset{x \to a}{\overset{Lt}{\longrightarrow}} f(x) = -\infty$ , then x = a is asymptote of y = f(x)If  $\underset{x \to +\infty}{Lt} f(x) = k$  or  $\underset{x \to -\infty}{Lt} f(x) = k$ , then y = k is asymptote of y = f(x)If  $\lim_{x \to \infty} \frac{f(x)}{x} = m_1$ ,  $\lim_{x \to \infty} (f(x) - m_1 x) = c$ , then  $y = m_1 x + c_1$  is an asymptote. (inclined to right) If  $\underset{x \to -\infty}{\text{Lt}} \frac{f(x)}{x} = m_2$ ,  $\underset{x \to -\infty}{\text{Lt}} (f(x) - m_2 x) = c_2$ , then  $y = m_2 x + c_2$  is an asymptote (inclined to left) Find asymptote of  $y = e^{-x}$  $\lim_{x \to \infty} y = \lim_{x \to \infty} e^{-x} = 0$ y = 0 is asymptote. Find asymptotes of xy = 1 and draw graph.  $y = \frac{1}{x}$ FREE Download Study Package from website: a control of the second study Package from  $\lim_{x \to 0} y = \lim_{x \to 0} \frac{1}{x} = \infty \Rightarrow x = 0 \text{ is asymptote.}$ y = 0 x = 0 $\lim_{x \to \infty} y = \lim_{x \to \infty} \frac{1}{x} = 0 \Rightarrow y = 0 \text{ is asymptote}$ Find asymptotes of  $y = x + \frac{1}{x}$  and sketch the curve. у  $\lim_{x \to 0} y = \lim_{x \to 0} \left( x + \frac{1}{x} \right) = +\infty \text{ or } -\infty$ = 2 x = 0 is asymptote.  $\lim_{x \to 0} y = \lim_{x \to 0} \left( x + \frac{1}{x} \right) = \infty$ = - 2  $\Rightarrow$ there is no asymptote of the type y = k.  $\lim_{x \to \infty} \frac{y}{x} = \lim_{x \to \infty} \left( 1 + \frac{1}{x^2} \right) = 1$  $\lim_{x \to \infty} (y - x) = \lim_{x \to \infty} \left( x + \frac{1}{x} - x \right) = \lim_{x \to \infty} \frac{1}{x} = 0$  $y = x + 0 \Rightarrow y = x$  is asymptote. A rough sketch is as follows Quadrature : If  $f(x) \ge 0$  for  $x \in [a, b]$ , then area bounded by curve y = f(x), x-axis, x-axis, x = a and x = b is  $\int f(x) dx$ 



Successful People Replace the words like; "wish", "try" & "should" with "I Will". Ineffective People don't.

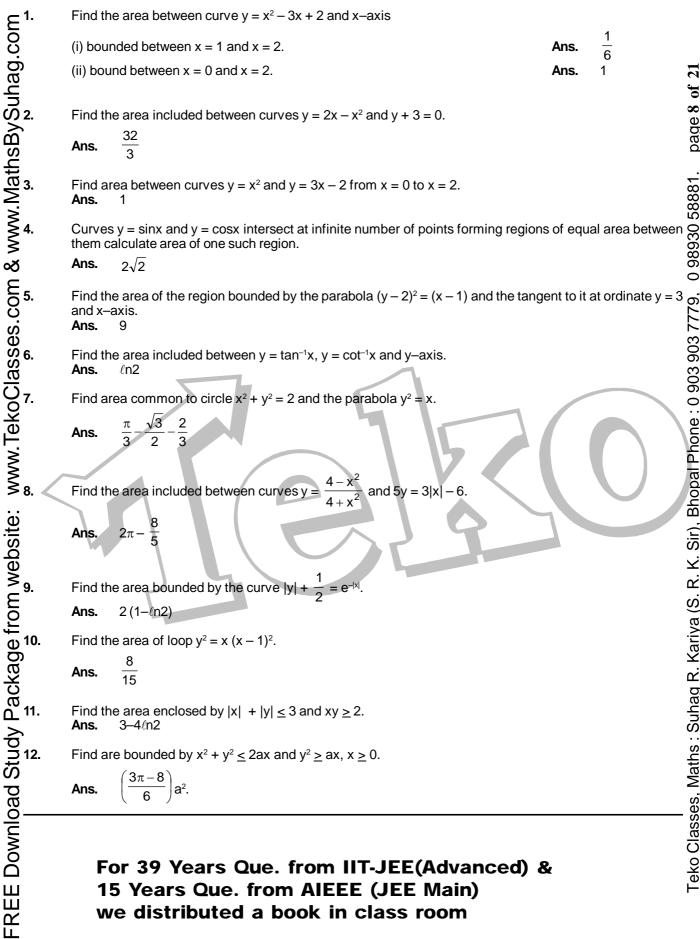




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 $x = \pm \frac{1}{\sqrt{2}}$ lf y = 0,FREE Download Study Package from website: www.TekoClasses.com & www.MathsBySuhag.com  $= \int_{-\infty}^{\sqrt{5}} \left( \frac{-3x + \sqrt{5 - x^2}}{5} - \frac{-3x - \sqrt{5 - x^2}}{5} \right) dx$ Required area  $=\frac{2}{5}\int_{-\pi}^{\sqrt{5}}\sqrt{5-x^2}\,dx$  $=\frac{4}{5}\int_{0}^{\sqrt{5}}\sqrt{5-x^2}dx$ Put x =  $\sqrt{5} \sin \theta$ : dx =  $\sqrt{5} \cos \theta d\theta$ L.L :  $x = 0 \Rightarrow \theta = 0$ U.L: x =  $\sqrt{5} \Rightarrow \theta = \frac{\pi}{2}$  $=\frac{4}{5}\int_{-\infty}^{\infty}\sqrt{5-5\sin^2\theta} \sqrt{5}\cos\theta d\theta$  $=4\int_{1}^{2}\cos^{2}\theta d\theta = 4\frac{1}{2}\frac{\pi}{2} = \pi$ Let A (m) be area bounded by parabola  $y = x^2 + 2x - 3$  and the line y = mx + 1. Find the least area Example : A(m). Solution. Solving we obtain  $x^{2} + (2 - m)x - 4 = 0$ Let  $\alpha,\beta$  be roots  $\Rightarrow \alpha + \beta = m - 2, \alpha\beta =$  $\int (mx+1-x^2-2x+3) dx$ A (m)  $\int (-x^2 + (m-2)x + 4) dx$  $=\left(-\frac{x^{3}}{3}+(m-2)\frac{x^{2}}{2}+4x\right)^{\beta}$  $= \left| \frac{\alpha^3 - \beta^3}{3} + \frac{m - 2}{2} (\beta^2 - \alpha^2) + 4(\beta - \alpha) \right|$  $= |\beta - \alpha|. \left| -\frac{1}{3}(\beta^2 + \beta\alpha + \alpha^2) + \frac{(m-2)}{2}(\beta + \alpha) + 4 \right|$  $= \sqrt{(m-2)^2 + 16} \left| -\frac{1}{3} \left( (m-2)^2 + 4 \right) + \frac{(m-2)}{2} (m-2) + 4 \right|$  $=\sqrt{(m-2)^2+16}$   $\left|\frac{1}{6}(m-2)^2+\frac{8}{3}\right|$  $=\frac{1}{6}\left((m-2)^2+16\right)^{3/2}$ A(m) Leas A(m) =  $\frac{1}{6}$  (16)<sup>3/2</sup> =  $\frac{32}{3}$ .

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