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Part : (A) Only one correct option 1. If (2:0) is the vertex & y - axis the directix of a parabola, then its focus is: (A) (2:0) (B) (-2:0) (C) (4:0) (D) (-4:0) (A) parabola is drawn with its focus at (3, 4) and vertex at the focus of the parabola y <sup>2</sup> - 12x - 4y + 4 = 0. The equation of the parabola is: (A) x <sup>2</sup> - 6x - 8y + 25 = 0 (B) y <sup>2</sup> - 8x - 6y + 25 = 0 (C) x <sup>2</sup> - 6x + 8y - 25 = 0 (D) x <sup>2</sup> + 6x - 8y - 25 = 0 (C) x <sup>2</sup> - 6x + 8y - 25 = 0 (D) x <sup>2</sup> + 6x - 8y - 25 = 0 (C) x <sup>2</sup> - 6x + 8y - 25 = 0 (D) x <sup>2</sup> + 6x - 8y - 25 = 0 (C) x <sup>2</sup> - 6x + 8y - 25 = 0 (D) x <sup>2</sup> + 6x - 8y - 25 = 0 (C) x <sup>2</sup> - 6x + 8y - 25 = 0 (D) x <sup>2</sup> + 6x - 8y - 25 = 0 (C) x <sup>2</sup> - 6x + 8y - 25 = 0 (D) x <sup>2</sup> + 6x - 8y - 25 = 0 (C) x <sup>2</sup> - 6x + 8y - 25 = 0 (D) x <sup>2</sup> + 6x - 8y - 25 = 0 (C) x <sup>2</sup> - 6x + 8y - 25 = 0 (D) x <sup>2</sup> + 6x - 8y - 25 = 0 (C) x <sup>2</sup> - 6x + 8y - 25 = 0 (D) x <sup>2</sup> + 6x - 8y - 25 = 0 (A) 8 \sqrt{3} (B) 6 \sqrt{3} (C) 4 \sqrt{3} (D) none (A) 8 \sqrt{3} (B) 6 \sqrt{3} (C) 4 \sqrt{3} (D) 2 \sqrt{3} 5. The circles on focal radii of a parabola as diameter touch: (A) the tangent at the vertex (B) the axis (C) the directrix (D) none of these (A) 8 $\sqrt{3}$ (B) $6 \sqrt{3}$ (C) $4 \sqrt{3}$ (D) $2 \sqrt{3}$ The equation of the tangent to the parabola y = (x - 3) <sup>2</sup> parallel to the chord joining the points 80 (A) 2x - 2y + 6 = 0 (B) 2y - 2x + 6 = 0 (C) 4y - 4x + 11 = 0 (D) 4x - 4y = 11 (A) $\frac{\pi}{4}$ (B) $\frac{\pi}{2}$ (C) $\frac{\pi}{3}$ (D) $\frac{\pi}{6}$ (A) $\frac{\pi}{4}$ (B) $\frac{\pi}{2}$ (C) $\frac{\pi}{2}$ (C) $\frac{\pi}{3}$ (D) $\frac{\pi}{6}$ (A) $\frac{\pi}{4}$ (B) $\frac{\pi}{2}$ (C) $\frac{\pi}{2}$ (D) $\frac{\pi}{2}$ + 4x at the points A & B. The co-ordinates of the point of intersection of the tangents drawn at the points A & B are: (A) $(\frac{\pi}{2}, \frac{5}{2})$ (B) $(\frac{-5}{2}, -\frac{7}{2})$ (C) $(\frac{5}{2}, \frac{7}{2})$ (D) $(-\frac{7}{2}, -\frac{5}{2})$ (D) AP & BP are tangents to the parabola, y <sup>2</sup> = 4x at the points A & B. The co-ordinates of the point of intersection of the tangents drawn at the points A & B are: (A) $(\frac{\pi}{2}, \frac{5}{2})$ (B) $(-\frac{5}{2}, -\frac{7}{2})$ (C) $(\frac{5}{2}, \frac{7}{2})$ (D) $(-\frac{7}{2}, -\frac{5}{2})$ (D) AP & BP are							
ŏ	1.	(A) $(2 \cdot 0)$ (B) $(-2 \cdot 0)$ (C) $(4 \cdot 0)$ (D) $(-4 \cdot 0)$ A parabola is drawn with its focus at (3, 4) and vertex at the focus of the parabola					
ag	2.	A parabola is drawn with its focus at $(3, 4)$ and vertex at the focus of the parabola $y^2 - 12x - 4y + 4 = 0$ . The equation of the parabola is:					
Ļ		(A) $x^2 - 6x - 8y + 25 = 0$ (B) $y^2 - 8x - 6y + 25 = 0$					
പ്	3	(C) $x^2 - 6x + 8y - 25 = 0$ The length of the chord of the parabola, $y^2 = 12x$ passing through the vertex & making an angle of $60^{\circ}$					
Š		with the axis of x is:					
SE	л	(A) 8 (B) 4 (C) $16/3$ (D) none The length of the side of an equilatoral triangle inseribed in the parabela, $y^2 = 4x$ so that one of its (0)					
ť	4.	The length of the side of an equilateral triangle inscribed in the parabola, $y^2 = 4x$ so that one of its of angular point is at the vertex is:					
N N		(A) $8\sqrt{3}$ (B) $6\sqrt{3}$ (C) $4\sqrt{3}$ (D) $2\sqrt{3}$					
Z.	5.	The circles on focal radii of a parabola as diameter touch:					
≶	6	(A) the tangent at the vertex (B) the axis (C) the directrix (D) none of these The equation of the tangent to the parabola $y = (x - 3)^2$ parallel to the chord joining the points (3, 0) and (4, 1) is:					
Š	0.	(3, 0) and $(4, 1)$ is:					
∞	7	(A) $2x - 2y + 6 = 0$ (B) $2y - 2x + 6 = 0$ (C) $4y - 4x + 11 = 0$ (D) $4x - 4y = 11$ The angle between the tangents drawn from a point (-a, 2a) to $y^2 = 4$ ax is $\pi$ $\pi$ $\pi$ $\pi$ $\pi$ $\pi$ $\pi$					
Е	7.	The angle between the tangents drawn nonra point $(-a, 2a)$ to $y^2 = 4 ax$ is					
8		(A) $\frac{\pi}{4}$ (B) $\frac{\pi}{2}$ (C) $\frac{\pi}{3}$ (D) $\frac{\pi}{6}$					
	8.	An equation of a tangent common to the parabolas $y^2 = 4x$ and $x^2 = 4y$ is					
0 O	٥	(A) $x - y + 1 = 0$ (B) $x + y - 1 = 0$ (C) $x + y + 1 = 0$ (D) $y = 0$ The line $4x - 7y + 10 = 0$ intersects the parabola, $y^2 = 4x$ at the points A & B. The co-ordinates of the					
ŝ	9.	point of intersection of the tangents drawn at the points A & B are:					
8		(A) $\left(\frac{7}{2}, \frac{5}{2}\right)$ (B) $\left(-\frac{5}{2}, -\frac{7}{2}\right)$ (C) $\left(\frac{5}{2}, \frac{7}{2}\right)$ (D) $\left(-\frac{7}{2}, -\frac{5}{2}\right)$ (B)					
쏫	10.	AP & BP are tangents to the parabola, $y^2 = 4x$ at A & B. If the chord AB passes through a fixed point $\bigcirc$					
Ĕ.							
≥	11.	Equation of the normal to the parabola, $y^2 = 4ax$ at its point (am <sup>2</sup> , 2 am) is:					
≶	10	(A) $y = -mx + 2am + am^3$ (B) $y = mx - 2am - am^3$ (C) $y = mx + 2am + am^3$ (D) none					
	12.	(A) $(4, 4)$ (B) $(9, 6)$ (C) $(4, -1)$ (D) $(1, 2)$					
 Ф	13.	At what point on the parabola $y^2 = 4x$ the normal makes equal angles with the axes? (A) (4, 4) (B) (9, 6) (C) (4, -1) (D) (1, 2) If on a given base, a triangle be described such that the sum of the tangents of the base angles is a $\frac{1}{100}$					
sit		constant, then the locus of the vertex is: (A) a circle (B) a parabola (C) an ellipse (D) a hyperbola					
ĝ	14.	A point moves such that the square of its distance from a straight line is equal to the difference $\sigma$					
Ň		between the square of its distance from the centre of a circle and the square of the radius of the circle.					
Ę		(A) a straight line at right angles to the given line (B) a circle concentric with the given circle <sup>L</sup> .					
õ	(C)a pa <b>15.</b>	arabola with its axis parallel to the given line( $D$ ) a parabola with its axis perpendicular to the given line. $\mathcal{O}$ P is any point on the parabola, $y^2 = 4ax$ whose vertex is A. PA is produced to meet the directrix in D & $\sigma$					
) fr	15.	M is the foot of the perpendicular from P on the directrix. The angle subtended by MD at the focus is: 🚖					
ge	16	(A) $\pi/4$ (B) $\pi/3$ (C) $5\pi/12$ (D) $\pi/2$					
á	16.	of the point of intersection of tangents at P & Q from the focus is:					
<u>S</u>	4 <del>7</del>	(A) 8 (B) 6 (C) 5 (D) 13 (D) 13					
Ъ	17.	(A) 8 (B) 6 (C) 5 (D) 13 Tangents are drawn from the point (-1, 2) on the parabola $y^2 = 4x$ . The length of intercept made by these tangents on the line $x = 2$ is:					
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n	18.	(A) 6 (B) $6\sqrt{2}$ (C) $2\sqrt{6}$ (D) none of these From the point (4·6) a pair of tangent lines are drawn to the parabola, $y^2 = 8x$ . The area of the triangle					
۲۲ ک		formed by these pair of tangent lines & the chord of contact of the point (4-6) is:					
σ	19.						
Оa		$y^2 = 4ax$ is					
Ы		$(A)(2a + x) y^2 + 4a^3 = 0$ $(B)(2a + x) + y^2 = 0$ $\overrightarrow{w}$ $(C)(2a + x) y^2 + 4a = 0$ $(D)$ none of these $\overrightarrow{O}$					
≥	20.	If the tangents & normals at the extremities of a focal chord of a parabola intersect at					
õ		$(x_1, y_1)$ and $(x_2, y_2)$ respectively, then:					
Ш	21.	Tangents are drawn from the points on the line $x - y + 3 = 0$ to parabola $y^2 = 8x$ . Then all the chords of					
Ш		contact passes through a fixed point whose coordinates are:					
Ĕ	22.	(A) $(3, 2)$ (B) $(2, 4)$ (C) $(3, 4)$ (D) $(4, 1)$ The distance between a tangent to the parabola $y^2 = 4 A x (A > 0)$ and the parallel normal with gradient					
ш		1 is:					
		(A) 4 A (B) $2\sqrt{2}$ A (C) 2 A (D) $\sqrt{2}$ A					
	23.	À variable parabola of latus ractum $\ell$ , touches a fixéd equal parabola, then axes of the two curves being					
	_						

Successful People Replace the words like; "wish", "try" & "should" with "I Will". Ineffective People don't.

Ge	parallel. The locus of	the vertex of the moving	curve is a parabola, wh	vw.MathsBySuhag.com
⊊ <sup>24.</sup>	(A) $\ell$ Length of the focal ch	(B) 2 $\ell$ ord of the parabola y <sup>2</sup> =	(C) 4 $\ell$ 4ax at a distance p from	(D) none n the vertex is:
Sor	(A) $\frac{2a^2}{2a^2}$	(B) $\frac{a^3}{2}$	(C) $\frac{4a^3}{2}$	(D) $\frac{p^2}{p}$
0. Dg 25.	) p	$p^2$	$p^2$	erpendicular to AB meeting the
eqr	axis at C. The project	ion of BC on the axis of	the parabola is	
ମ୍ ୪୦ 26.		(B) 2a f the perpendiculars dra	(C) 4a wn from the vertex on a	(D) 8a variable tangent to the parabola 🛐
Э. Э.	$y^{2} = 4ax$ is: (A) $x (x^{2} + y^{2}) + ay^{2} =$	0	(B) y $(x^2 + y^2) + ax^2 =$	0 10
07 11 27.	$(C) \times (x^2 - y^2) + ay^2 =$ T is a point on the tang	ent to a parabola y <sup>2</sup> = 4a	(D) none of these ax at its point P. TL and T	N are the perpendiculars on the $\stackrel{\circ}{\mathbb{Q}}$
Ma	focal radius SP and th (A) SL = 2 (TN)	e directrix of the parabo	la respectively. Then: (C) SL = TN	(D) 2 (SL) = 3 (TN)
<u>≥</u> <sup>28.</sup>	The point of contact	t of the tangent to the angle θ with the axis of	e parabola y <sup>2</sup> = 9x wh the parabola such that	ich passes through the point tan $\theta > 2$ is
≩ 29.	(A) (4/9, 2)	(B) (36, 18) (and x <sup>2</sup> = 32 y intersect a	(C) (4, 6)	(D) (1/4, 3/2) 8
ά δ	(3)	(4)	. , _	. o
E 30.	(A) $\tan^{-1}\left(\frac{1}{5}\right)$	(B) $\tan^{-1}\left(\frac{1}{5}\right)$	(C) $\pi$	(D) $\frac{\pi}{2}$ abola, y <sup>2</sup> = 4x. If $\theta_1 \& \theta_2$ are the O
www.TekoClasses.com & www.MathsBySuhag.com 35 35 36 38 32 39 35 35 34			π	
ses	(A) $x - y + 1 = 0$	angents with the axis of $(B) x + y - 1 = 0$	(C) $x - y - 1 = 0$	, then the locus of P is: $(D) x + y + 1 = 0$
ທີ່ 31.	Locus of the point of	intersection of the norm	Tails at the ends of para	llel chords of gradient m of the e
Ö	parabola $y^2 = 4ax$ is: (A) $2 xm^2 - ym^3 = 4a$ (	$(B) 2 \times m^2$ (B) $2 \times m^2 \times m^2$	$n^3 = 4a(2 + m^2)$	803 9 03
0 옷 32.	The equation of the o		bola y <sup>2</sup> = 4a (2 – m <sup>2</sup> ) bola y <sup>2</sup> = 4ax which pas	ses through the intersection of $\overset{\widetilde{o}}{\circ}$
μ. Έ	those at (4a, – 4a) & ( (A) 5x – y + 115 a = 0	9a, – 6a) is: (B) 5x + y – 135 a = 0	(C) $5x - y - 115a = 0$	(D) 5x + y + 115 = 0
<b>≩</b> 33.	The point(s) on the pa x <sup>2</sup> + y <sup>2</sup> - 24y + 128 =	arabola y² = 4x which ar 0 is/are:	e closest to the circle,	Pho
$\geq$	(A) (0, 0)	(B) $(2, 2\sqrt{2})$	(C) (4, 4)	(D) $5x + y + 115 = 0$ (D) none chords $P_1P_2$ and $Q_1Q_2$ intersect on $H_1$
<sup>34.</sup>	If $P_1Q_1$ and $P_2Q_2$ are t the	wo focal chords of the par	Tabola $y^2 = 4ax$ , then the c	shords $P_1P_2$ and $Q_1Q_2$ intersect on $\frac{Q}{m}$
bsite	(A) directrix	(B) axis nal to $y^2 = 12x$ , then k is	(C) tangent at the verte	
→ 36.	(A) 3	(B) 9	(C) –9	(D) - 3
> 30. E	x-axis is			nd the parabola $y^2 = 4x$ above the $\vec{H}$ [IIT - 2001]
froi	(A) $\sqrt{3}y = 3x + 1$	(B) $\sqrt{3}y = -(x + 3)$	(C) $\sqrt{3}y = x + 3$	
ອ 37.	The focal chord to y <sup>2</sup> : chord are:	= 16 x is tangent to $(x - 6)$	$(5)^{2} + y^{2} = 2$ , then the pos	sible values of the slope of this [IIT - 2003]
ka	(A) {- 1, 1}	(B) {- 2, 2}	(C) {- 2, 1/2}	(D) {2, - 1/2}
ပ္ရ 38.	The normal drawn at a	point $(at_1^2, -2at_1)$ of the particular point (at_1^2, -2at_1) of the part	arabola y² = 4ax meets it a	again in the point (at <sup>2</sup> , 2at ), then [ <b>IIT - 2003]</b>
<u>с</u> >	$(\Lambda)$ t $-$ t $+$ $\frac{2}{-}$	(B) $t_2 = t_1 - \frac{2}{t_1}$	$(C) t = t + \frac{2}{2}$	
nq		-	- 1	$(D) t_2 - t_1 - \frac{C}{t_1} \qquad \qquad$
び <sup>39.</sup>	The angle between the	tangents drawn from the	point (1, 4) to the parabo	again in the point (at $_{2}^{2}$ , 2at ), then [fIT - 2003] (D) $t_{2} - t_{1} - \frac{2}{t_{1}}$ (D) $\frac{\pi}{6}$ (D) $\frac{\pi}{6}$ (D) $\frac{\pi}{6}$ (D) $\frac{y^{2}}{4} + 4x + 2 = 0$ (D) $y^{2} + 4x + 2 = 0$
ad	(A) $\frac{\pi}{2}$	(B) $\frac{\pi}{3}$	(C) $\frac{\pi}{4}$	(D) $\frac{\pi}{6}$
0 U 40.		) and Q a point of the loc	4	mid point of PQ is
NO		(B) $x^2 - 4y + 2 = 0$		[IIT - 2005] (D) y2 + 4x + 2 = 0
FREE Download Study Package from wek		. , -		ig the line $y = x$ . If the distances
	•	s from the origin are resp	vectively $\sqrt{2}$ and 2 $\sqrt{2}$ , t	then an equation of the parabola
ЦЦ	IS (A) $(x + y)^2 = x - y + (C) (x - y)^2 = 8(x + y)^2$	2	(B) $(x - y)^2 = x + y - x^2$ (D) $(x + y)^2 = 8(x - y)^2$	2 2
	$(\cup) (x - y)^{2} = \delta(x + y)^{2}$	<i>−∠</i> )	$(D) (x + y)^2 = 8(x - y)^2$	+ 2)

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E		Let ABCD be a square of side length 2 units. $C_2$ is the circle through vertices A, B, C, D and $C_1$ is the circle touching all the sides of the square ABCD. L is a line through A.	
J.CC	42.	If P is a point on C <sub>1</sub> and Q in another point on C <sub>2</sub> , $\frac{PA^2 + PB^2 + PC^2 + PD^2}{QA^2 + QB^2 + QC^2 + QD^2}$ is equal to [IIT - 2006]	
าลดู		(A) 0.75 (B) 1.25 (C) 1 (D) 0.5	
Sul	43.	A circle touch the line L and the circle C, externally such that both the circles are on the same side of the line, then the locus of centre of the circle is [IIT - 2006]	۶I
www.TekoClasses.com & www.MathsBySuhag.com	44.	(A) ellipse (B) hyperbola (C) parabola (D) parts of straight line A line M through A is drawn parallel to BD. Point S moves such that its distances from the line BD and the vertex A are equal. If locus of S cuts M at T <sub>2</sub> and T <sub>3</sub> and AC at T <sub>1</sub> , then area of $\Delta$ T <sub>1</sub> T <sub>2</sub> T <sub>3</sub> is <b>[IIT - 2006)</b> ]	
athe			page
ž	Dart · (	B) May have more than one options correct	_
'.	45.	If any and of a facel shared of the neuropole $y^2 = 4y$ is $(1, 0)$ the other and lies on	<u>.</u>
Ş	46.	(A) $x^2 y + 2 = 0$ (B) $xy + 2 = 0$ (C) $xy - 2 = 0$ (D) $x^2 + xy - y - 1 = 0$ The tangents at the extremities of a focal chord of a parabola	2000
<pre></pre>	-10.	(A) are perpendicular (B) are parallel	ñ D
2 S	47.	(C) intersect on the directrix (D) intersect at the vertex If from a variable point 'P' pair of perpendicular tangents PA and PB are drawn to any parabola then	0 98930
on		(A) P lies on directrix of parabola (B) chord of contact AB passes through focus	л С
0		(D) P lies on director circle	-
ês	48.	A normal chord of the parabola subtending a right angle at the vertex makes an acute angle $\theta$ with the $x - axis$ , then $\theta = 0$	"
SS			20
<u>Ja</u>		(A) arc tan 2 (B) arc sec $\sqrt{3}$ (C) arc cot $\sqrt{2}$ (D) $\frac{\pi}{2}$ - arc cot $\sqrt{2}$	803
8	49.	Variable chords of the parabola $y^2 = 4ax$ subtend a right angle at the vertex. Then: (A) locus of the feet of the perpendiculars from the vertex on these chords is a circle	903
e K		(B) locus of the middle points of the chords is a parabola	2
Ŀ.	50.	(C) variable chords passes through a fixed point on the axis of the parabola $(D)$ none of these Two parabolas have the same focus. If their directrices are the x – axis & the y – axis respectively, then	Phone
Ş	~	the slope of their common chord is:	5
¥	51.		
		P is a point on the parabola $y^2 = 4ax$ (a > 0) whose vertex is A. PA is produced to meet the directrix in $\overline{D}$ and M is the foot of the perpendicular from P on the directrix. If a circle is described on MD as a diameter then it intersects the x-axis at a point whose co-ordinates are:	ģ
it€		(A) (-3a, 0) (D) $(-a, 0)$ (C) $(-2a, 0)$ (D) $(a, 0)$	•
q Q		EXERCISE-11	
website:	1. 2.	Find the vertex, axis, focus, directrix, latusrectum of the parabola $x^2 + 2y - 3x + 5 = 0$ .	Ż
	Ζ.	Find the set of values of $\alpha$ in the interval [ $\pi/2$ , $3\pi/2$ ], for which the point (sin $\alpha$ , cos $\alpha$ ) does not lie outside the parabola $2y^2 + x - 2 = 0$ .	
ē	3.	Two perpendicular chords are drawn from the origin 'O' to the parabola $y = x^2$ , which meet the parabola at P 9 and O Bectangle POOR is completed. Find the locus of vertex B	ת ש
ef	4.	Find the equation of tangent & normal at the ends of the latus rectum of the parabola	<u>S</u> LIS
ag	5.	$y^2 = 4a (x - a)$ . Prove that the straight line $\ell x + my + n = 0$ touches the parabola $y^2 = 4ax$ if $\ell n = am^2$ .	Ž
Š	6.	Two perpendicular chords are drawn from the origin. O to the parabola $y = x^2$ , which meet the parabola at P $\leq$ and Q Rectangle POQR is completed. Find the locus of vertex R. Find the equation of tangent & normal at the ends of the latus rectum of the parabola $y^2 = 4a$ (x - a). Prove that the straight line $\ell x + my + n = 0$ touches the parabola $y^2 = 4ax$ if $\ell n = am^2$ . If tangent at P and Q to the parabola $y^2 = 4ax$ intersect at R then prove that mid point of R and M lies on the parabola, where M is the mid point of P and Q. Find the equation of normal to the parabola $x^2 = 4y$ at (9, 6). Find the equation of the chord of $y^2 = 8x$ which is bisected at (2, -3) Find the locus of the mid-points of the chords of the parabola $y^2 = 4ax$ which subtend a right angle at the vertex of the parabola.	с D
ğ	7.	Find the equation of normal to the parabola $x^2 = 4y$ at (9, 6).	Шa
ц Т	8. 9.	Find the equation of the chord of $y^2 = 8x$ which is bisected at $(2, -3)$ Find the locus of the mid-points of the chords of the parabola $y^2 = 4ax$ which subtend a right angle at the $\cdot$	กี
, D	40	vertex of the parabola.	2
St	10.	Find the focus of the mid-points of the chords of the parabola $y^2 = 4ax$ which subtend a right angle at the vertex of the parabola. Find the equation of the circle which passes through the focus of the parabola $x^2 = 4y$ & touches it at the point (6, 9). Prove that the normals at the points, where the straight line $\ell x + my = 1$ meets the parabola $y^2 = 4ax$ , meet on the normal at the point $\left(\frac{4am^2}{\ell^2}, \frac{4am}{\ell}\right)$ of the parabola.	Na
g	11.	Prove that the normals at the points, where the straight line $\ell x + my = 1$ meets the parabola $y^2 = 4ax$ ,	je Se
00		meet on the normal at the point $\left(\frac{4am^2}{4am}\right)$ of the parabola	<b>JSS</b>
lu	40	$\left(\begin{array}{c} \ell^2 & \ell \end{array}\right) = \left(\begin{array}{c} \ell^2 & \ell \end{array}\right) = \left(\begin{array}{c} \ell^2 & \ell \end{array}\right)$	5
Download Study Package from	12.	that SP. SQ . SR = a. SO <sup>2</sup> .	
	13.	Show that the locus of the point of intersection of the tangents to $y^2 = 4ax$ which intercept a constant length $r$	-
FREE	14.	d on the directrix is $(y^2 - 4ax) (x + a)^2 = d^2 x^2$ . Show that the distance between a tangent to the parabola $y^2 = 4ax$ and the parallel normal is	
Ē	15.	a sec <sup>2</sup> $\theta$ cosec $\theta$ , where $\theta$ is the inclination of the either with the axis of the parabola. P and Q are the point of contact of the tangents drawn from a point R to the parabola $y^2 = 4ax$ . If PQ be a	
		normal to the parabola at P, prove that PR is bisected by the directrix.	
	16.	A circle is described whose centre is the vertex and whose diameter is three-quarters of the latus rectum of the parabola $y^2 = 4ax$ . If PQ is the common chord of the circle and the parabola and L, L <sub>2</sub> is	

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the latus rectum, then prove that the area of the trapezium  $PL_1L_2Q$  is

- 17. If the normals from any point to the parabola  $x^2 = 4y$  cuts the line y = 2 in points whose abscissa are in A.P., then prove that slopes of the tangents at the 3 conormal points are in GP.
- 18. Prove that the length of the intercept on the normal at the point (at<sup>2</sup>, 2at) made by the circle which is
- described on the focal distance of the given point as diameter is a  $\sqrt{1+t^2}$ 63 of 91 19. A parabola is drawn to pass through A and B, the ends of a diameter of a given circle of radius a, and to have as directrix a tangent to a concentric circle of radius b; then axes being AB and a perpendicular

 $\frac{x^2}{b^2} + \frac{y^2}{b^2 - a^2} = 1$ diameter, prove that the locus of the focus of the parabola is

23.

- PNP' is a double ordinate of the parabola then prove that the locus of the point of intersection of the 20. normal at P and the straight line through P' parallel to the axis is the equal parabola
- $y^2 = 4a (x 4a).$ Find the locus of the point of intersection of those normals to the parabola  $x^2 = 8 y$  which are at right  $\bigotimes_{x=2}^{\infty}$  angles to each other. 21.
- Let C<sub>1</sub> and C<sub>2</sub> be respectively, the parabolas  $x^2 = y 1$  and  $y^2 = x 1$ . Let P be any point on C<sub>1</sub> and Q be the reflections of P and Q, respectively, with respect to the line  $\overset{\circ}{\text{D}}_{2} = x$ . Prove that P<sub>1</sub> lies on C<sub>2</sub>, Q<sub>1</sub> lies on C<sub>1</sub> and PQ  $\geq$  min {PP<sub>1</sub>, QQ<sub>1</sub>}. Hence or otherwise determine  $\overset{\circ}{\text{D}}_{2} = x$ . Prove that P<sub>1</sub> lies on C<sub>2</sub>, Q<sub>1</sub> lies on C<sub>1</sub> and PQ  $\geq$  min {PP<sub>1</sub>, QQ<sub>1</sub>}. Hence or otherwise determine  $\overset{\circ}{\text{D}}_{2} = x$ . Prove that P<sub>1</sub> lies on C<sub>2</sub>, Q<sub>1</sub> lies on C<sub>1</sub> and C<sub>2</sub> respectively such that P<sub>0</sub> Q<sub>0</sub>  $\leq$  PQ for all pairs of points O(P, Q) with P on C<sub>1</sub> and Q on C<sub>2</sub>. 22.
  - Normals are drawn from the point P with slopes  $m_1, m_2, m_3$  to the parabola  $y^2 = 4x$ . If locus of P with  $x^2 = 4x$ .  $m_2 m_2 = \alpha$  is a part of the parabola itself then find  $\alpha$ . [IIT - 2003]

nswers

Download Study Package from website: www.TekoClasses.com & www.MathsBySuhag.com EXERCISE-EXERCISE-10 1. С 2. 3. 4 6 D 7. B <u>3</u>, –  $\left(\frac{29}{8}\right)$ , focus  $\left(\frac{3}{2}\right)$ 1. vertex ≡ 8. С 9. 13. B 14. D С 10. A 11. A 12. D axis x = 3, directrix y =  $-\frac{29}{3}$ . Latus rectum = 2 19. A 20. C 21. C 15. D 16. B 17. B 18. C 22. B 25. C 26. A 27. C  $y^2 = x - 2$ 23. B 24. C 28. A 2.  $\alpha \in [\pi/2, 5\pi/6] \cup [\pi, 3\pi/2]$ 3. Tangent y = x, y = -x,29. A 30. C 32. B 33. C 34. A 35. B 31. A Normal x + y = 4a, x - y = 4a37. A 36. C 39. B 40. C **41.** C 38. A **42.** A 7. 2x + 9y = 72**8.** 4x + 3y + 1 = 0 $y^2 - 2ax + 8a^2 = 0$ 9. 43. C 44. C 46. AC 47. ABCD 45. ABD **10.**  $x^2 + y^2 + 18x - 28y + 27 = 0$ 48. BD 49. ABC 50. AB 51. AD **21.**  $x^2 - 2y + 12 = 0$ **23.** α = 2