

ANSWER

Exercise - 1

- | | | |
|------------------------|---------|-------|
| 1. B | 2. D | 3. C |
| 4. 4.8 Ma ² | 5. 1/√2 | |
| 6. B | 7. D | 8. D |
| 9. A | 10. D | 11. C |
| 12. D | 13. C | 14. C |
| 15. C | 16. D | 17. C |
| 18. C | 19. D | 20. B |
| 21. AC | 22. D | 23. D |
| 24. C | 25. A | 26. D |
| 27. C | 28. B | 29. C |
| 30. C | 31. D | 32. C |
| 33. A | 34. D | 35. B |
| 36. A | 37. D | 38. A |
| 39. B | 40. D | 41. A |
| 42. B | 43. D | |

Exercise - 2

SECTION (A) :

- A 1. 20 s
 A 2. (a) $\langle \omega \rangle = 2a / 3 = 4 \text{ rad/s}$;
 $\langle \beta \rangle = \sqrt{3ab} = 6 \text{ rad/s}^2$;
 (b) $\beta = 2\sqrt{3ab} = 12 \text{ rad/s}^2$.

A 3. $t = \sqrt[3]{(4/a) \tan \alpha} = 7 \text{ s}$

SECTION (B) :

- B 1. (i) $I = \frac{al^4}{4}$ (ii) $\frac{al^4}{36}$
 B 2. $1.5 \times 10^{-3} \text{ kg-m}^3, 4.0 \times 10^{-3} \text{ kg-m}^3$
 B 3. $\frac{100}{1000} (1^2 + 2^2 + 3^2 + \dots) \times 10^{-6} = 0.43 \text{ kg-m}^2$
 B 4. $\frac{MR^2}{2} - M \left(\frac{4R}{3\pi} \right)^2$ B 5. $\frac{M\ell^2}{3}$
 B 6. $\frac{14 m r^2}{5}$
 B 7. $\sqrt{\frac{1}{m} \left(I - \frac{m\ell^2}{12} \right)} = \sqrt{\frac{7}{60}} = 0.34 \text{ m}$
 B 8. (a) $I = (1/2) \pi p b R^4 = 2.8 \text{ g.m}^2$
 B 9. $I = m (a^2 + b^2)$ B 10. $ma^2/12$
 B 11. $\sqrt{2} r$ B 12. $r/\sqrt{2}$
 B 13. $\frac{2\rho a^7}{21}$ B 14. $\frac{m\ell^2}{6}$
 B 15. (a) $2\pi \left(\frac{Aa^4}{4} + \frac{Ba^5}{5} \right)$

B 16. (b) $I = 3/10 mR^2$

SECTION (C) :

C 1. $N = (aB - bA)k$, where k is the unit vector of

the z axis $\ell = |aB - bA| / \sqrt{A^2 + B^2}$

C 2. $\ell = |aB - bA| / \sqrt{A^2 + B^2}$

C 3. $v_2 = v_1 \frac{r_1 \rho_1 \eta_2}{r_2 \rho_2 \eta_1} = 5 \mu\text{m/s}$

SECTION (D) :

D 1. $P = \frac{W}{2} \cot \theta$ or $P = \frac{mg}{2} \cot \theta$

D 2. 76 g, 42 g, $\frac{21}{38}$.

D 3. 1.04 N in the left string and 1.12 N in the right

D 4. 43 N

D 5. (a) $T = 225 \text{ N}$ (b) $F_x = 225 \text{ N}, F_y = 300 \text{ N}$

D 6. $\frac{L \cos \theta \sin^2 \theta}{2h - L \cos^2 \theta \sin \theta}$

D 7. $\frac{3W}{8}$

SECTION (E) :

E 1. $\frac{3Ft^2}{2m\ell}$

E 2. (a) $\frac{2g(m_1 - m_2)}{\ell(m_1 + m_2)} = \frac{60}{7} = 8.4 \text{ rad/s}^2$

(b) (i) $\frac{2g(m_1 - m_2)}{\ell(m_1 + m_2 + m_3/3)} = \frac{90}{22} = 8.0 \text{ rad/s}^2$,

(ii) $(m_1 g - m_1 \alpha \frac{\ell}{2}) = 29 \text{ N}$;

$(m_2 g + m_2 \alpha \frac{\ell}{2}) = 27.6 \text{ N}$

E 3. (a) $\frac{3g}{4L}$ (cw) (b) $N = \frac{13mg}{16}$ ↑,

$F = \left(\frac{3\sqrt{3}}{16} \right) mg \rightarrow$ (c) $\frac{3\sqrt{3}}{13}$

E 4. (a) $\frac{3g}{2\sqrt{2}\ell}$ (cw) (b) $\frac{3}{2} g \downarrow$ (c) $\frac{Mg}{4}$ ↑

E 5. (a) $\frac{g}{7} \text{ m/s}^2$ (b) 0.125 m/s^2

E 6. (a) $\frac{g}{11}$ (b) $\frac{20g}{31} \text{ N}$

E 7. $T = 1/2mg, a = gmr^2/I$

E 8. (a) $\frac{213}{73}$ m/s ↓ (b) 40.9 N

E 9. $\tau = 3/4 \omega R/\text{kg}$. E 10. $\langle \omega \rangle = 1/3 \omega_0$

E 11. $x = \frac{2L}{3}$

E 12. $\frac{M}{m} = \sqrt{15}$

SECTION (F) :

F 1. $\sqrt{\frac{3g}{\ell}} = 5.4 \text{ rad/s}$ F 2. $w = \sqrt{5} \text{ rad/s}$

F 3. $\frac{1}{19} \sqrt{380g}$ F 4. $\omega = \sqrt{\frac{9g}{4\ell}}$

F 5. 0.5 m/s F 6. $\alpha = \frac{3g \cos \theta}{2\ell}$

SECTION (G) :

G 1. $0.9\sqrt{2} \text{ dm}$

G 2. (a) $T = 2mg$ (b) $N = 6mg$ (c) $\frac{3g}{5L}$ (d) $\sqrt{\frac{6g}{5L}}$

SECTION (H) :

H 1. $16 \text{ kg m}^2/\text{s}$ H 2. $2\hat{k} \text{ kg m}^2/\text{s}$

H 3. $0.5 \text{ kg-m}^2/\text{s}, 75 \text{ J}$

H 4. 19.7 rad/s H 5. 2.4 rad/s

H 6. 0.04 kg-m^2 H 7. 12 rad/s

H 8. $\omega = \frac{45}{14} = 3.21 \text{ rad/s (ccw)}, v_s = \frac{1}{7} 0.143 \text{ m/s}$

H 9. $\frac{4\pi m}{M+2m}$ H 10. 6.3 m/s

H 11. 41°

H 12. (a) $\omega = \frac{12V}{7L}$ (b) $v = \frac{7}{12} \sqrt{2gL} = 3.5 \text{ m/s}$

H 13. 0.8 rev/s

SECTION (I) :

I 1. (a) $\frac{4v_0}{3}$ (b) $\frac{5v_0}{3\ell}$ (c) $v_x = \frac{v_0}{2}, v_y = \frac{2v_0}{3}$

I 2. (a) $w_A = v^2 / R = 2.0 \text{ m/s}^2$, the vector w_A is permanently directed to the centre of the wheel ; (b) $s = 8R = 4.0 \text{ m}$

I 3. $\frac{7}{10} mv^2$

I 4. (a) $v_A = 2\omega t = 10.0 \text{ cm/s}$,
 $v_B = \sqrt{2} \omega t = 7.1 \text{ cm/s}, v_0 = 0$;

(b) $\omega_A = 2\omega \sqrt{1 + (\omega t^2/2R)^2} = 5.6 \text{ cm/s}^2$,

$\omega_B = \omega \sqrt{1 + (1 - \omega t^2/R)^2} = 2.5 \text{ cm/s}^2$,

$\omega_0 = \omega^2 t^2 / R = 2.5 \text{ cm/s}^2$

I 5. $R_A = 4r, R_B = 2\sqrt{2} r$

I 7. $3m$

SECTION (J) :

J 1. 50 m/s

J 2. (a) 300 mm from A

(b) $\alpha = 4.00 \text{ rad/s}^2$ (ccw) ; $\bar{a} = 1.800 \text{ m/s}^2 \rightarrow$

J 3. $\frac{\omega \ell}{6} \text{ m/s}, \frac{\ell}{6} \text{ m}$ below the centre of the rod

J 4. $\sqrt{10gh/7}$ J 5. $\frac{3v^2}{4g}$

J 6. $\sqrt{\frac{10}{7} g \ell \sin \theta}$ J 7. 17 mg/7

J 8. $v = \sqrt{\frac{14gR}{3}}$

J 9. (a) 1.633 N (b) 1.224 m

J 10. (a) $T = w$ (b) $\alpha = rg/k^2$ (ccw)

J 11. $\frac{2}{3} g$ J 12. (a) $\frac{2}{5} \tan \theta$ (b) $\frac{7}{8} mg \sin \theta$

J 13. 3.3 N J 14. $\frac{25}{9} \text{ m/s} \leftarrow$

J 15. $\ell = 2aF_2/mw = 1.0$

J 16. (i) (a) $3g/L$ (cw)

(b) $\left(\frac{\sqrt{3}}{2} \hat{i} + \hat{j}\right) g = 1.323g \angle 49.1^\circ$

(c) $\left(\frac{\sqrt{3}}{2} \hat{i} - 2\hat{j}\right) g = 2.18g \angle -66.6^\circ$

(ii) (a) g/L (cw) (b) $-\left(\frac{\sqrt{3}}{2}\right) g \hat{i}$

(c) $-\left(\frac{\sqrt{3}}{2} \hat{i} + \hat{j}\right) g = 1.323g \angle -130.9^\circ$

J 17. (a) $\theta = \cos^{-1} \frac{4}{7}$ (b) $v = \sqrt{\frac{4}{7} gr}$ (c) $\frac{k_T}{k_R} = 6$

J 18. $\sqrt{\frac{27}{7} g(R-r)}$

J 19. (a) $mg(H-R-R \sin \theta)$, (b) $\frac{10}{7} g \left(\frac{H}{R} - 1 - \sin \theta\right)$,

$-\frac{5}{7} g \cos \theta$ (c) $4.9 \text{ N}, 0.196 \text{ N}$ upward

Exercise - 3

- J 20. (i) (a) $\frac{1.2g}{\ell}$ (cw) (b) $-0.3(\hat{i} + 2\hat{j})$ g
 (ii) (a) 24g/17ℓ (cw) (b) 12g/17ℓ
 (iii) 2.4g/ℓ (cw) (b) 0.5gℓ

J 21. $\frac{9\pi + 16}{18\pi}$

J 22. $F_{\max} = 3\text{kg}/(2 - 3\text{k}); \quad w_{\max} = 2\text{kg}/(2 - 3\text{k})$

J 23. $w = 3g(M + 3m) / (M + 9m + I/R^2)$

SECTION (K) :

K 1. (a) $v = 0$ (b) $\omega = \frac{v}{5a}$ (c) $\frac{3}{5} mv^2$

K 2. $\frac{v_0}{3}$ (\leftarrow), $\frac{2v_0}{3}$ (\rightarrow)

K 3. (a) $\frac{Ft}{m}$ (b) $\frac{6Ft}{m\ell}$ (c) $\frac{2F^2t^2}{m}$ (d) $\frac{F\ell t}{2}$

K 4. $\frac{\pi L}{12}$

K 5. $\omega = \frac{1.7v}{2R}$ $v_{\min} = \frac{2}{1.7} \sqrt{0.3gR}$

K 6. 2R/3 above the centre

K 7. $\omega R/3$ K 8. $3v/5$

K 9. (a) $\frac{5v_0}{2r}$ (ccw) (b) $\frac{v_0}{\mu_k g}$

K 10. (a) $t = \frac{6a\pi}{\sqrt{3}v_0}$

(b) $s = \frac{a}{\sqrt{3}} \sqrt{1 + (2\pi + \sqrt{3})^2}$

K 11. (a) $\frac{mL\sqrt{gh}}{\sqrt{2}}$, $\sqrt{\frac{8gh}{3L}}$ (b) $\frac{3}{2} L$

K 12. $3v/7$

K 13. $\omega = \frac{v_1}{L} \frac{12\sin\beta}{3\sin^2\beta + 1}$ (cw)

K 14. $H = \left(\frac{1 - 3\cos^2\theta}{1 + 3\cos^2\theta} \right)^2$; $h = \frac{49\pi\ell}{144}$

SECTION (L) :

L 1. $\frac{1}{2} mg a \sin\theta$

1. (a) $v = \frac{2v_0}{3}$; $t_0 = \frac{v_0}{3} \mu g$

(b) $w = -\mu mg (v_0 t - \frac{3}{2} \mu g t^2)$; $-\frac{1}{6} mv_0^2$

2. $\frac{mg}{6}$, up

3. (a) 6 N

(b) $\vec{\tau}_1 = 0.6\hat{k} - 0.6\hat{j}$, $\vec{\tau}_2 = -0.6\hat{k} - 0.6\hat{j}$

4. B

5. 4.8 Ma²

6. $w(d-x)/d$, wx/d

7. (a) $\vec{F} = \frac{2mV}{\Delta t} \hat{i} - \frac{2mV}{\sqrt{3}\Delta t} \hat{k}$; $\vec{N} = \left(\frac{2mV}{\sqrt{3}\Delta t} + mg \right) \hat{k}$,

(b) $\vec{\tau} = -\left(\frac{4mVh}{\sqrt{3}\Delta t} \right) \hat{j}$

8. $v = \sqrt{5gR}$

9. A

10. A, B, C

11. C

12. C

13. (a) $a_c = \frac{4F}{3m_1 + 8m_2}$; $a_p = \frac{8F}{3m_1 + 8m_2}$

(b) friction at the top of the cylinder = $3m_1 F / (3m_1 + 8m_2)$ towards right, friction at the bottom = $m_1 F / (3m_1 + 8m_2)$ towards right

14. A

15. C

16. D

17. B

18. (a) $\frac{m}{M} = \frac{1}{4}$

(b) $AP = \frac{2L}{3}$ (c) $v_p = \frac{v_0}{2\sqrt{2}}$

19. A

20. A

21. $\theta = 60^\circ$

22. B

23. A

24. (a) $x = 0.1$ m (b) $\omega = 1$ rad/s (c) never

25. B

26. B

27. (a) $\sqrt{3} m \omega^2 \ell$

(b) $F_y = \sqrt{3} m \omega^2 \ell$ $F_x = -F/4$

28. A

29. C

30. B

31. B

32. B

33. B

34. B

35. $\frac{3mv}{\ell(M+3m)}$

36. A

37. C, D

38. A, B